

A Kinetic Model of Municipal Sludge Degradation During Non-catalytic Wet Oxidation

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Abstract

Wet oxidation is a successful process for the treatment of municipal sludge. In addition, the resulting effluent from wet oxidation is a useful carbon source for subsequent biological nutrient removal processes in wastewater treatment. Owing to limitations with current kinetic models, this study produced a kinetic model which predicts the concentrations of key intermediate components during wet oxidation. The model was regressed from lab-scale experiments and then subsequently validated using data from a wet oxidation pilot plant. The model was shown to be accurate in predicting the concentrations of each component, and produced good results when applied to a plant 500 times larger in size. A statistical study was undertaken to investigate the validity of the regressed model parameters. Finally the usefulness of the model was demonstrated by suggesting optimum operating conditions such that volatile fatty acids were maximised.

Keywords: Wet oxidation, municipal sludge, kinetic modelling, wastewater

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1 **1. Introduction**

2 Municipal sludge is the semi-solid residue remaining at the end of a munic-
3 ipal wastewater treatment process. The treatment of municipal sludge is be-
4 coming increasingly important as current disposal methods such as landfill are
5 not sustainable, G et al. (2005), and regulations surrounding sludge disposal are
6 becoming more restrictive, (an indicative example being Potts (2003)). This is
7 intensifying the search for alternative disposal and treatment processes that can
8 address the unique challenges that municipal sludge present, in particular the
9 high water content and the presence of pathogens.

10 One attractive wastewater treatment alternative is wet oxidation. Wet ox-
11 idation is the liquid phase treatment of organic or oxidisable inorganic com-
12 pounds at elevated temperature and pressure, typically using using oxygen as
13 an oxidant (applied as air or pure oxygen gas). The typical range of reaction
14 conditions for wet oxidation are 150 to 320°C at 20 to 150 bar of pressure and a
15 residence time of 15 to 120 minutes Zou et al. (2007). A historical review of wet
16 oxidation for the treatment of pulpmill liquors and subsequently for wastewater
17 sludge treatment over the last 40 years is given in Debellefontaine & Foussard
18 (2000).

19 Given that wet oxidation does not require water removal prior to treatment,
20 it can directly process liquid municipal sludge. Furthermore the high tempera-
21 tures involved kill the pathogens present and sterilise the material. While the
22 wet oxidation process has been the focus of numerous studies Van Amstel & Ri-
23 etema (1973); Li et al. (1991); Mishra et al. (1995); Debellefontaine & Foussard
24 (2000), there are still relatively few models that describe the kinetic behaviour of
25 the intermediate and final products of municipal sludge under different reaction
26 conditions needed for an in-depth process analysis.

27 The first stage in the wet oxidation of sludge involves a large proportion of
28 the insoluble organic content being solubilised through hydrolytic depolymeri-
29 sation. Subsequent oxidative reactions convert these hydrolysis products into

30 increasingly simpler organics such as acetic acid and formic acid, and acetone
31 and ash. Finally these products can be further oxidised to CO₂, water and
32 residual ash, Bernardi et al. (2010); Debellefontaine & Foussard (2000).

33 The reaction pathways that occur under wet oxidation are complex and
34 poorly characterised. Even wet oxidation of pure substances such as phenol have
35 been shown to decompose via numerous reaction pathways, and therefore it is
36 necessary to use a simplified kinetic model which only includes the dominant
37 reaction pathways Moreno et al. (2012); Zhang & Chuang (1999). Because
38 of this, simplified lumped kinetic models, often employing pseudo-components
39 such as Chemical Oxygen Demand (COD) in the kinetic model, are used to
40 conveniently describe the wet oxidation process.

41 The variety of previously proposed lumped parameter models for the wet
42 oxidation of a range of waste products, (including municipal sludge) is evident
43 from the range of models listed in Table 1. Van Amstel & Rietema (1973) was
44 one of the first to propose a lumped model for municipal sludge. This early
45 work was further expanded by other researchers Foussard et al. (1989); Li et al.
46 (1991); Khan et al. (1999); Shanableh (2004) who investigated different oper-
47 ating conditions and proposed modifications to the kinetic pathways. Li et al.
48 (1991) proposed the familiar generalised lumped kinetic model for municipal
49 sludge which forms the basis for the development of the kinetic model proposed
50 in this work.

51 Historically, the primary outcome of wet oxidation applied to municipal
52 waste was complete oxidation to the final end products which are mainly CO₂,
53 water and residual solids, Mishra et al. (1995). However with wastewater treat-
54 ment plants incorporating Biological Nutrient Removal (BNR) facilities becom-
55 ing more common, the short chain acids which are an intermediate product of
56 wet oxidation, can be used as an effective carbon source for the denitrifying
57 bacteria, Djafer et al. (2000); Shanableh & Jomaa (2005); Strong et al. (2011);
58 Andrews et al. (2014); Baroutian et al. (2015).

59 While models like that proposed by Li et al. (1991) give information on the
60 rate of solids or COD reduction and acetic acid production, they generally lack

Table 1: Summary of published wet oxidation kinetic models. (See also Table 2.)

Investigators	Feed material	Model inputs	Reaction pathways	Validated states
Takamatsu et al. (1970)	Mixture of peptone, glucose & metal salts	O ₂ , T	3	3
Van Amstel (1971)	Municipal sludge	O ₂ , T, P	2	1
Foussard et al. (1989)	Municipal sludge	O ₂ , T	2	1
Li et al. (1991)	Municipal sludge	O ₂ , T	3	1
Khan et al. (1999)	Municipal sludge	O ₂ , T	4	4
Zhang & Chuang (1999)	Kraft pulp sludge	O ₂ , T	2	1
Verenich & Kallas (2002); Verenich et al. (2003)	Pulp mill liquor	O ₂ , T	4	1
Shanableh (2004)	Municipal sludge	O ₂ , T	2	2
Chacuk & Imbierowicz (2007)	Municipal sludge	O ₂ , T	4	0
Mucha & Zarzycki (2008)	Municipal sludge	T	4	1
Bertanza et al. (2014)	Municipal sludge	O ₂ , T	3	2
<i>This work</i>	Municipal sludge	O ₂ , T, P, RPM	12	7

61 detailed modelling of the intermediate products produced, such as the fate of
62 nitrogen based compounds. The additional load of these intermediate products
63 in the liquid effluent produced by a wet oxidation facility has the potential to
64 upset downstream biological treatment processes. This provides the motivation
65 to develop a more comprehensive model that can better predict the fate of these
66 intermediate compounds.

67 Despite the fact that wet oxidation liquor is a useful supplement for a BNR
68 treatment plant, and generalised kinetic models of wet oxidation are available,
69 none of the dynamic models in Table 1 adequately describe the spectrum of in-
70 termediate products, and the conditions under which they are produced. Con-
71 sequently there is a need for more detailed kinetic models describing wet ox-
72 idation which characterise sufficiently the concentrations of the intermediate
73 compounds, such that potential impact on a downstream biological treatment
74 plant can be predicted. Therefore, this paper proposes a detailed kinetic model
75 for wet oxidation of municipal sludge which can predict the concentration of
76 intermediate products which are important to BNR processes under different
77 reaction conditions.

78 Table 2 compares the kinetic structure of the key lumped kinetic models
79 noted in Table 1 starting with the basic Li et al. (1991) model similar to that
80 presented in (Bertanza et al., 2014, Table 3). In all models, the variable k_i is
81 an Arrhenius based rate expression. The species symbols used are the same as
82 the original references. In the models presented by Mucha & Zarzycki (2008)
83 and Bertanza et al. (2014), S are the feedstock particular organic compounds,
84 L, L_1 are intermediate liquid products, and G_i and L_k, L_2 refers to gaseous and
85 non biodegradable liquid products respectively. It is clear from the topology
86 that while they may appear different, from a mechanistic viewpoint they are
87 related, and descend from the Li *et al* model. Each model starts with an initial
88 compound which is degraded or solubilised to an intermediate product. This is
89 then oxidised to one or more reaction end products. For comparison, the model
90 presented in this work is given in Fig. 3.

91 However there are some deficiencies of these mechanistic models which was

Table 2: Comparison of published wet oxidation kinetic pathways.

Diagram	Reference
<pre> graph TD A -- k1 --> B A -- k2 --> C B -- k3 --> C </pre>	Li et al. (1991)
<pre> graph LR VTS --> CH2O VTS --> NH3 VTS --> VFAs CH2O --> sCOD NH3 --> sCOD VFAs --> sCOD </pre>	Khan et al. (1999)
<pre> graph LR S --> G1 S --> L G1 -- k1 --> G2 L -- k2 --> Lk </pre>	Mucha & Zarzycki (2008)
<pre> graph LR S -- k1 --> L1 L1 -- k2 --> G L1 -- k3 --> L2 </pre>	Bertanza et al. (2014)

92 the motivating factor to develop a more comprehensive model and to undertake
93 experiments to investigate the effect of temperature, oxygen partial pressure
94 and mixing in the form of stirrer speed, on the degradation of biosolids under
95 wet oxidation. The currently available kinetic models (such as those presented
96 in Table 2) do not typically take into account the effect of all the operational
97 parameters. Furthermore it was important to be able to track the nitrogenous
98 species.

99 In summary, this paper's contribution is the development of a kinetic model
100 based on the results of the lab scale experimental programme, to validate the
101 model against pilot-plant data and to explore optimum operating points.

102 **2. Materials and Methods**

103 The municipal biosolids feed material used for the experiments was obtained
104 from the Rotorua Lakes Council (RLC) wastewater treatment plant. Rotorua
105 is a medium sized rural town of 70,000 and is typical of many municipalities in
106 New Zealand. The biosolids consisted of approximately 40% primary and 60%
107 secondary sludge obtained from the belt presses at the processing plant. The
108 biosolids were subsequently fermented in a 2000L pilot plant anaerobic fermenter
109 at 35°C under pH control of between 5.5 and 6.2. Samples of the fermented
110 sludge were frozen at -20°C until required. For this study, the following metrics
111 were of particular interest: Total Suspended Solids (TSS), Volatile Suspended
112 Solids (VSS), Total COD (tCOD), Particulate COD (pCOD), Soluble COD
113 (sCOD), Acetic Acid COD (AACOD), Dissolved Organic Nitrogen (DON). The
114 characteristics of the sludge used in the experiments are shown in Table 3.

115 For this study, experiments were performed on two wet oxidation systems: a
116 laboratory scale stirred reactor used to develop and regress the dynamic model,
117 and a pilot plant employing a 300L bubble column reactor used purely for
118 validation.

Table 3: Characteristics of the diluted municipal biosolids from the RLC wastewater treatment plant used for the experimental investigation.

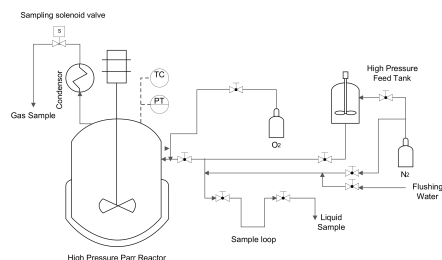
Characteristics	[mg/L]
TSS	14872±542
VSS	12082±440
tCOD	24720±901
pCOD	17640±643
sCOD	7080±258
Acetic acid	1364±50
Propionic acid	664±24
Iso-butyric acid	143±5
N-butyric acid	542±20
NH ₄	470±10
DKN	560±12
TC	7000±100
TN	1200±20

119 *2.1. Lab Scale Reactor Procedure*

120 Wet oxidation experiments were carried out in a Parr high pressure reactor
121 (model # 4540. Parr Instrument Company, USA) with model # 4848 controller
122 as described in Baroutian et al. (2015). The experimental system depicted in
123 Fig. 1 was equipped with a pre-heated feed vessel in which 150 mL of sludge
124 slurry was heated to 90°C for 5 minutes with stirring. This minimised the
125 temperature differential associated when the sample was transferred to the re-
126 actor. In order reduce the possibility of hydrolysis reactions occurring during
127 the heat up stage, the sludge was injected to the reactor only when the vessel
128 had reached the desired temperature. This control system is PID controller
129 with auto-tuning capability which is able to precisely control temperature with
130 a minimum overshoot.

131 For each experiment the reactor was charged with 250 mL water and was ini-
132 tially pressurised with pure oxygen (20–40 bar) to obtain an oxygen to biomass
133 ratios of 1:1 to 2:1. These ratios were calculated based on the stoichiometric
134 oxidation potential using assumed biomass composition of $\text{CH}_{1.8}\text{O}_{0.5}\text{N}_{0.2}$. It
135 was then heated to 220 to 240°C before the pre-heated sludge was introduced
136 by means of pressure difference generated by nitrogen gas back pressure. After
137 the injection of sludge, the initial concentration of solids in the reactor was ap-
138 proximately 1.5 wt%. The experiments were carried out using stirring speeds
139 ranging from 300 to 500 revolutions per minute (RPM) corresponding to power
140 numbers, P_o , of 128 to 27. The mixing was fully turbulent with the Reynolds
141 number, $Re > 10^5$. The use of RPM as a variable as opposed to Reynolds num-
142 ber or energy dissipation for describing turbulence is purely pragmatic since it
143 is easier to measure. In any case, as will be evident in section 3, this variable
144 had negligible effect on the model.

145 Using a manual extraction system, 20 mL liquid samples were taken after 2,
146 5, 10, 20 and 60 minutes. The sampling tube was flushed with water followed
147 by nitrogen gas after each sample was collected. Samples were cooled to room
148 temperature immediately to stop further reaction. A total of 18 experiments
149 were conducted following a fractional factorial design, exploring different com-



(a) Diagram of lab scale Parr reactor



(b) Photograph of Parr reactor and sampling system

Figure 1: The bench-scale Parr reactor

Figure 2: The pilot plant reactor

150 binations of temperature, oxygen partial pressure and stirring speed with the
 151 center of the design space repeated 4 times.

152 Gas samples from the reactor headspace were taken for four of the experi-
 153 ments using a high pressure Valco selector valve, which directed the gas through
 154 a cooler, reducing the temperature of the samples to 10°C. The gas samples of
 155 approximately 20mL volume were collected in Tedlar gas sample bags for later
 156 analysis.

157 2.2. Pilot Plant

158 Wet oxidation experiments were performed on a semi-batch pilot plant facil-
 159 ity to validate the results from the lab scale investigation, Andrews et al. (2015);
 160 Lei et al. (2013); Aggrey et al. (2011). The pilot plant, shown in Fig. 2 consists
 161 of a 300L bubble column reactor utilising co-current gas and liquid recirculation
 162 to promote mixing of the two phases.

163 An important difference in operating procedure between the bench-scale and
 164 pilot reactors was the requirement to use a continuous flow of oxygen in the pilot

165 plant. PID control was used to maintain the oxygen concentration in the reactor
166 headspace to between 20 and 25%. It was not possible to operate the reactor
167 in fully batch mode with pure oxygen in the reactor due to safety concerns. A
168 second difference is that the laboratory reactor is mechanically stirred, while
169 the pilot plant relies on gas recirculation to provide the mixing.

170 The feed tank was filled with municipal sludge which was the same source of
171 feed material for the lab scale experiments. Water was added to dilute the feed
172 to the required concentration of 1.5% solids. Approximately 150kg of biosolids
173 were then pumped into the main reactor, which was then pressurised to 20 bar
174 using compressed air, and the heating and circulation systems were started.
175 After the initial pressurisation, pure oxygen was used to maintain the oxygen
176 concentration in the reactor to between 20 and 25%.

177 After the temperature had reached the required setpoint, liquid samples of
178 the reactor contents were taken approximately every 15 minutes and immedi-
179 ately quenched to stop further reactions, while the oxygen concentration was
180 continuously sampled as part of the reactor control system. Other gasses apart
181 from oxygen were not measured on the pilot plant due to equipment constraints.

182 *2.3. Analysis Procedure*

183 Liquid samples collected in this study were analysed for COD (total COD,
184 soluble COD and particulate COD), solids (TSS and VSS), VFAs, NH_4 and
185 DKN (dissolved Kjeldahl nitrogen). The analysis procedure followed stan-
186 dard methods recommended by the American Public Health Association Anon
187 (1998). The tCOD used in this work was calculated following the procedure by
188 Baroutian et al. (2013) because of the large variability in the tCOD measure-
189 ment. This discrepancy is suspected to be due to the inhomogeneous nature of
190 the intermediate samples.

191 *2.4. Kinetic Modelling of Wet Oxidation*

192 A common family of intermediate compounds are produced during the wet
193 oxidation process. These are primarily short chain volatile fatty acids and dis-
194 solved nitrogen in the form of ammonia. As mentioned in Section 1, the focus

195 of this study was to develop kinetic models that characterise the degradation of
 196 sludge and the production of intermediate compounds. For this study, several
 197 COD based pseudo-compounds were postulated to characterise the behaviour
 198 observed from the experimental data, with many being common wastewater
 199 quality indicators and are shown in Table 4. This simplification is in line with
 200 previous work such as Li et al. (1991) and Zhang & Chuang (1999).

201 For this study, the following pseudo-components were of particular interest,
 202 particulate COD (pCOD), soluble COD (sCOD), acetic acid (AACOD), volatile
 203 fatty acids (VFACOD), dissolved organic nitrogen (DON) and CO₂.

Table 4: A summary of the measured and derived state variables in the extended model.

State variables	Derived state variables	Measured states
pCODfast	pCOD=pCODfast+pCODslow	pCOD
pCODslow	sCOD=sCODfast+sCODslow+sCODnr	sCOD
sCODfast	VFACOD=VFAfast+VFAslow	VFACOD
sCODslow	O _{2(aq)}	DON
sCODnr		AACOD
AACOD		O _{2(g)}
VFACODfast		CO ₂
VFACODslow		
DON		
O _{2(g)}		
CO ₂		

204 Based on the results obtained from this experimental study, and the kinetic
 205 models available in the literature, a new set of 12 reaction pathways has been
 206 proposed. A lumping approach has been used and the reaction species are
 207 characterised in terms of their COD.

208 Like Shanableh (2004), the current study proposed that biosolids particles in
 209 the form of pCOD are first transformed into sCOD, and it is the sCOD which is

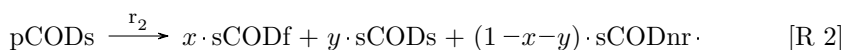
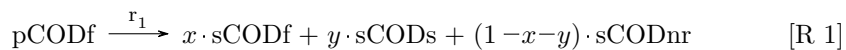
210 then oxidised into acetic acid, other VFA's, and a portion is oxidised directly to
 211 CO₂. The VFACOD component accounts for all other VFAs such as propionic
 212 acid which were observed to degrade under the reaction conditions in this study.

213 The analysis of the experimental data revealed that pCOD and sCOD con-
 214 sisted of multiple fractions. This phenomena was also noted previously by Shan-
 215 ableh who denoted the fractions of pCOD and sCOD as difficult to degrade and
 216 easy to degrade.

217 In this study, pCOD and sCOD have been subdivided into fast reacting
 218 (CODf) and slow reacting (CODs) fractions, while sCOD also has a non-reacting
 219 remainder, (CODnr). These have thus been denoted as pCODf, pCODs, sCODf,
 220 sCODs and sCODnr in the reaction pathways. The fractions for pCOD and
 221 sCOD were regressed to fit the experimental data.

222 The following reaction pathways are proposed following the kinetic pathway
 223 given in Fig. 3 to describe wet oxidation of municipal sludge and are imple-
 224 mented as ordinary differential equations (ODEs) in the model.

Particulate COD first solubilises into soluble COD following reactions R1
 and R2



Particulate COD is assumed to hydrolyse into fast and slowly solubilising frac-
 tions, and the reactions are assumed not to consume oxygen. The nitrogen
 containing fraction of pCOD is assumed to solubilise to DON,



Figure 3: The kinetic pathway for the proposed model in this study. (See also Table 2 for previously proposed kinetic pathways.)

Soluble COD then oxidises as shown in reactions R4 to R12



These reactions are subject to the following algebraic mass constraints

$$\text{sCOD} = \text{sCODf} + \text{sCODs} + \text{sCODnr}$$

$$\text{pCOD} = \text{pCODf} + \text{pCODs}$$

$$\text{VFACOD} = \text{VFACODf} + \text{VFACODs}$$

$$1 = x + y, \quad (x, y > 0)$$

$$0 < j < 1$$

where x , y and z are the fractions of fast reacting, slow reacting and non-reactive soluble COD, and j are the fractions of fast and slowly reacting VFA.

The reaction rate r in reactions R1 to R12 is assumed of the form

$$r_i = [\text{C}][\text{O}_{2(\text{aq})}]^n k_i \exp\left(\frac{-E_a}{RT}\right) N^c \quad (1)$$

225 Where $[\text{C}]$ and $[\text{O}_{2(\text{aq})}]$ are the reactant and oxygen concentrations, n is the reac-
 226 tion order with respect to oxygen, k_i is the rate constant (in variable units), E_a is
 227 the activation energy (Jmol^{-1}), R is the ideal gas constant ($8.3145 \text{ JK}^{-1}\text{mol}^{-1}$),
 228 T is temperature (Kelvin), N is the stirrer speed (RPM) and c is the mixing

229 constant (dimensionless). The kinetic equation is based on the work of Li et al.
230 (1991); Debellefontaine & Foussard (2000). The effect of oxygen has been in-
231 cluded for all reactions, except the solubilisation of pCOD, to attempt to ac-
232 count for other un-modelled reaction pathways or effects that may be occurring.
233 Further simplifications include no gas-liquid mass transfer limitations and the
234 reactant order was hard-coded as 1 following the work of Li et al. (1991).

235 Reactions R 3 and R 12 deserve some comment. While the formation of am-
236 moniacal nitrogen is not modelled with strict mechanistically accuracy, these
237 reactions allow the tracking of nitrogenous species conversion. This approach
238 was justified by the fact that the DON measurement itself is not describing
239 a molecule, but the presence of an element within a group of unknown com-
240 pounds, these latter contributing to the overall substrate COD. In this work,
241 we attributed the nitrogen containing COD to the slowly degradable particulate
242 fraction.

243 The effect of stirrer speed changes was accounted for by a power law based on
244 the work of Meille et al. (2004) who demonstrated that it adequately captured
245 the effects of the change in stirrer speed. Henry’s law was used internally in
246 the model to predict the concentration of dissolved oxygen based on the current
247 operating conditions, Himmelblau (1960).

248 The act of sampling was accounted for as part of the reactor model developed
249 in this study because of the moderate change in liquid volume during the course
250 of the experiments as the result of sampling.

251 *2.5. Parameter Regression*

252 The kinetic model developed in the previous section consists of a total of 12
253 reactions, 11 states, 3 derived states, and a number of other parameters which
254 need to be fitted. Each reaction has a total of 4 free parameters.

255 In order to have sufficient fitting data, the data from all experiments per-
256 formed on the lab scale reactor for this study was used and fitted simultaneously.
257 This results in a total of 266 ordinary differential equations, and 52 free param-
258 eters. The number of equations is primarily a function of how many experiments

259 were carried out, and the number of parameters stems from the complexity of
260 the model. Notwithstanding the problem is over defined.

261 The resultant nonlinear dynamic regression problem was solved using are
262 solved using LN_COBYLA algorithm from the `nlopt` package which is part of the
263 OPTI toolbox, Currie & Wilson (2012); Currie (2014) within the MATLAB en-
264 vironment, taking around 4 hours to complete on a modern desktop computer.
265 Given that this regression problem is both nonlinear and of high dimension,
266 there is both the problem of local minima and that the parameters in the Ar-
267 rhenius expression could easily be correlated meaning that the response contours
268 are highly elliptical. It is impractical to completely remove these two problems,
269 but they can be mitigated by scaling the regression problem prior to the optimi-
270 sation, and by carefully choosing the initial guesses of the fitted variables, and
271 subsequently repeating the optimisation from different starting points to avoid
272 local minima. All three approaches were taken in this study.

273 Further details on the regression algorithm, starting conditions and conver-
274 gence criteria are given in Prince-Pike (2014).

275 An increased weighting has been applied to the final $t = 60$ value of pCOD to
276 further improve the fit because of the large range between the initial and final
277 pCOD concentrations. The confidence limits of the fitted parameters can be
278 approximated using a linearised analysis following the strategy given in section
279 6.4 of Himmelblau (1970). The final values of the fitted kinetic parameters along
280 with 95% confidence limits are presented in the following section.

281 **3. Results and Discussion**

282 To adequately cover the variable space, a fractional factorial experimental
283 design was used as described in Prince-Pike (2014). Of the 18 experiments
284 undertaken for this study, Figures 4 to 5 compare the model prediction against
285 measured data for the components of interest for a subset of four different sets
286 of reaction conditions. In these plots, the points indicate the experimentally
287 measured concentrations while the curves show the regressed model predictions.

288 The values and uncertainty limits of the model parameter values (parameters
289 in the kinetics equations, and initial fractions of the compounds) are given in
290 Table 5.

291 The results in Figure 4 show the change in total, particulate and suspended
292 COD (tCOD, pCOD and sCOD) over 60 minutes for four different scenarios,
293 and the corresponding model predictions. The O₂ content listed is based on
294 the amount of initial pure oxygen in the reactor. The final COD removal rates
295 of between 53 and 61% obtained in this experiment agrees with similar stud-
296 ies, Chung et al. (2009); Lendormi et al. (2001); Shanableh (2004) as does the
297 particulate COD removal previously reported by Shanableh (2004). The error
298 bars show that there is greater uncertainty in the early samples due to the inho-
299 mogeneous nature of the early samples, hence the justification to preferentially
300 weight the later samples, particularly the final measured value which was known
301 to a higher relative accuracy. Although the peak sCOD values are marginally
302 higher in this work, the trend of sCOD evolution during the experiments was
303 similar to Chung et al. (2009).

304 Figure 5 shows the change in AACOD and VFACOD for the same reaction
305 conditions. While there is more variation in the results compared to pCOD
306 and sCOD, the model still fits the data, however the fit for the early samples
307 at 2 and 5 minutes is not as good. Apart from this discrepancy, the trend for
308 AACOD and VFA degradation follows published results by Chung et al. (2009).

309

310 *3.1. A Statistical Assessment of Model Quality*

311 Given that the proposed model has more fitted parameters than previously
312 proposed models, it is prudent to test if the extra complication is statistically
313 justified. Table 5 lists all the fitted parameters and their associated 95% confi-
314 dence limits. The fact that none of the parameter uncertainties span across zero
315 gives an indication that all parameters are deemed statistically significant. With
316 the exception of one parameter, k_0 for Reaction 5 at 44%, all uncertainties are
317 less than 30% of the nominal value. The confidence limits were not calculated

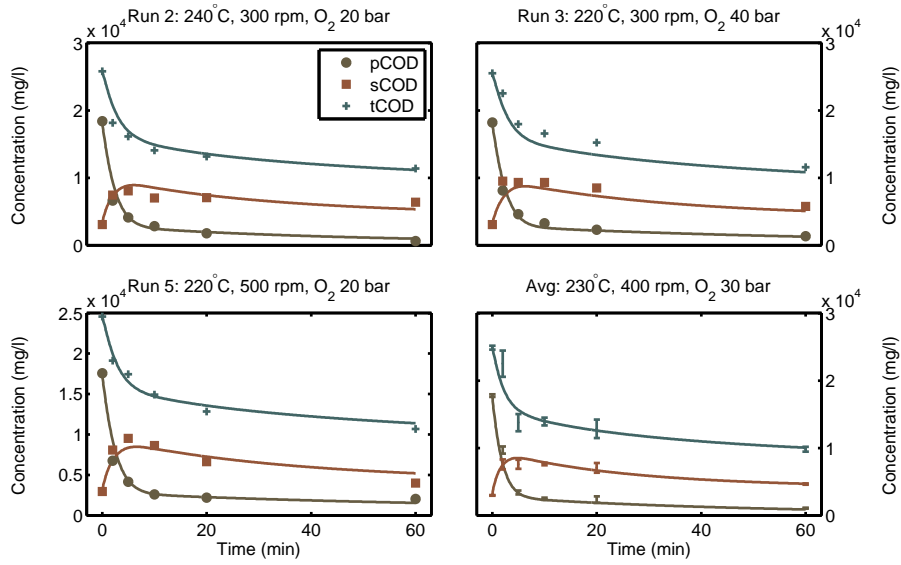


Figure 4: The concentration of particulate, suspended and total COD compared to model predictions during wet oxidation at four sets of reaction conditions.

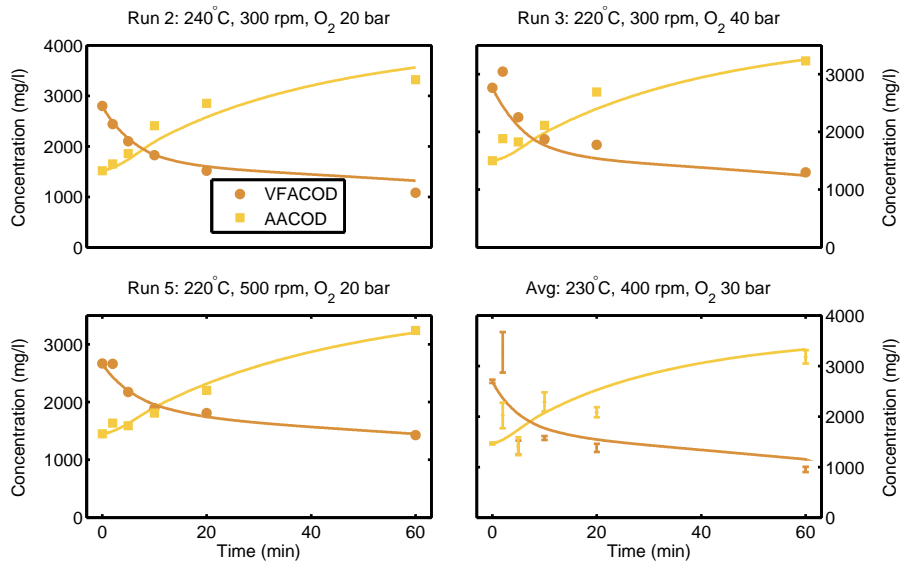


Figure 5: The concentration of AACOD and VFACOD during wet oxidation at four sets of reaction conditions.

318 for Reaction 8 because of the limited involvement at these reaction conditions,
319 as such it was not included to reduce the number of parameters used.

320 The correlations for the main components of interest between the model
321 predictions and actual measurements are given separately in Figure 6 for the
322 important variables. In this case the initial conditions are shaded grey and
323 are not included in the calculation for the individual correlation coefficient, r^2 ,
324 noted in the subfigures because they were explicitly used as initial conditions in
325 the parameter fitting.

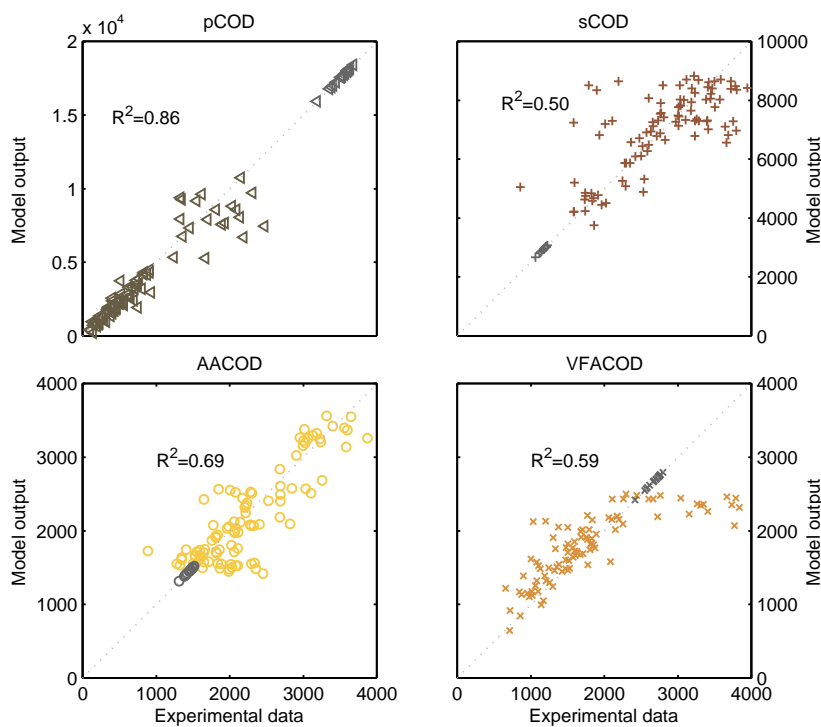


Figure 6: The correlation between model and experiment for the key individual components from the lab scale experiments.

326 The ANOVA analysis in Table 5 shows that all of the 47 parameters tested
327 were significantly different from zero, indicated by the t values being non-zero,
328 and that the parameters were statistically significant as all p values were much
329 smaller than the value of 0.05 corresponding to the 95% confidence limit chosen

330 as the cut-off for this analysis.

Table 5: The fitted model parameters, their associated 95% confidence limits and statistical
331 metrics. E_a is measured in J/mol.

Reaction		θ at 95%	Std error	t value	p value
Rxn 1	k	$(1.78 \pm 0.46) \times 10^3$	2.35×10^2	7.59	1.82×10^{-13}
	E_a	$(4.03 \pm 0.40) \times 10^4$	1.90×10^3	21.26	7.49×10^{-70}
	n	0.30 ± 0.10	0.05	6.23	1.10×10^{-9}
	c	0.47 ± 0.10	0.05	9.22	1.16×10^{-18}
Rxn 2	k	$(3.08 \pm 0.96) \times 10^6$	4.89×10^5	.30	7.31×10^{-10}
	E_a	$(1.25 \pm 0.08) \times 10^5$	4.28×10^3	29.18	1.16×10^{-105}
	n	0.45 ± 0.13	0.07	6.57	1.40×10^{-10}
	c	0.74 ± 0.31	0.16	4.59	5.66×10^{-6}
Rxn 3	k	$(5.91 \pm 2.18) \times 10^2$	1.11×10^2	5.33	1.56×10^{-7}
	E_a	$(4.88 \pm 0.59) \times 10^4$	2.99×10^2	16.33	2.25×10^{-47}
	n	0.56 ± 0.17	0.09	6.44	3.04×10^{-10}
	c	0.06 ± 0.02	0.01	5.01	7.86×10^{-7}
Rxn 4	k	$(1.76 \pm 0.49) \times 10^3$	2.49×10^2	7.09	5.38×10^{-12}
	E_a	$(3.53 \pm 0.40) \times 10^4$	2.03×10^3	17.37	4.78×10^{-52}
	n	0.30 ± 0.08	0.04	7.31	1.26×10^{-12}
	c	0.47 ± 0.11	0.06	8.45	4.18×10^{-16}
Rxn 5	k	$(3.87 \pm 1.73) \times 10^5$	8.81×10^4	4.40	1.36×10^{-5}
<i>Continued on next page</i>					

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Table 5 – continued from previous page

Reaction	θ at 95%	Std error	t value	p value	
	E_a	$(1.07 \pm 0.08) \times 10^5$	3.93×10^3	27.26	3.65×10^{-97}
	n	0.93 ± 0.30	0.15	6.03	3.35×10^{-9}
	c	1.18 ± 0.26	0.13	8.94	1.02×10^{-17}
Rxn 6	k	$(7.40 \pm 1.83) \times 10^2$	9.31×10^1	7.94	1.62×10^{-14}
	E_a	$(6.04 \pm 0.68) \times 10^4$	3.44×10^3	17.55	7.56×10^{-53}
	n	0.89 ± 0.23	0.12	7.57	2.18×10^{-13}
	c	0.55 ± 0.14	0.07	7.88	2.47×10^{-14}
Rxn 7	k	$(2.91 \pm 0.87) \times 10^2$	4.43×10^1	6.57	1.41×10^{-10}
	E_a	$(4.79 \pm 0.54) \times 10^4$	2.75×10^3	17.44	2.41×10^{-52}
	n	0.25 ± 0.09	0.04	5.66	2.70×10^{-8}
	c	0.46 ± 0.13	0.07	6.84	2.61×10^{-11}
Rxn 8	k	1.64×10^0	–	–	–
	E_a	1.84×10^5	–	–	–
	n	0.13	–	–	–
	c	0.02	–	–	–
Rxn 9	k	$(1.26 \pm 0.36) \times 10^1$	0.02	6.91	1.69×10^{-11}
	E_a	$(3.76 \pm 0.60) \times 10^4$	3.03×10^2	12.42	1.27×10^{-30}
	n	0.31 ± 0.10	0.05	5.97	4.89×10^{-9}
	c	0.55 ± 0.22	0.11	4.84	1.77×10^{-6}
Rxn 10	k	$(8.42 \pm 3.3) \times 10^2$	1.66×10^2	5.09	5.39×10^{-7}
	E_a	$(3.52 \pm 0.41) \times 10^4$	2.06×10^3	17.07	1.07×10^{-50}
<i>Continued on next page</i>					

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Table 5 – concluded from previous page

Reaction		θ at 95%	Std error	t value	p value
	n	0.37 ± 0.14	0.07	5.23	2.63×10^{-7}
	c	0.06 ± 0.03	0.02	3.49	5.33×10^{-4}
Rxn 11	k	$(9.67 \pm 3.30) \times 10^1$	1.67×10^1	5.82	1.10×10^{-8}
	E_a	$(4.36 \pm 0.76) \times 10^4$	3.88×10^3	11.25	5.08×10^{-26}
	n	0.34 ± 0.21	0.11	3.22	1.37×10^{-3}
	c	0.40 ± 0.13	0.07	6.03	3.49×10^{-9}
Rxn 12	k	$(1.21 \pm 0.44) \times 10^1$	2.27	5.34	1.48×10^{-10}
	E_a	$(3.06 \pm 0.68) \times 10^4$	3.47×10^3	8.82	2.55×10^{-17}
	n	0.79 ± 0.26	0.13	5.93	5.96×10^{-9}
	c	$0.17 \pm 0.07 \times 10^{-2}$	3.63×10^{-4}	4.66	4.26×10^{-6}
<i>Initial conditions for state variables</i>					
pCOD fast		0.84			
pCOD slow		0.16			
sCOD fast		0.5 ± 0.05	0.02	21.6	7.30×10^{-70}
sCOD slow		0.30 ± 0.05	0.03	11.46	7.42×10^{-27}
sCOD nr		0.20			
VFACOD fast		0.49 ± 0.11	0.06	8.60	1.39×10^{-16}
VFACOD slow		0.51			

334

335 The extremely small p value for the ANOVA summary in Table 6 demon-
336 strates that it is highly unlikely that all model coefficients are zero.

337 Table 7 gives the overall fit of the extended kinetic model. The high values for
338 R^2 and the adjusted R^2 show that the model is able to describe the variation
339 observed in the experimental data with a reasonable level of accuracy. The
340 actual values of the sum of squared errors, and the root-mean-square error are
341 scale dependent, (so difficult to compare in general sense) but are commonly
342 stated in an analysis of variance.

343 Overall, the model is shown to predict the likely concentrations of the compo-
344 nents of interest with a good level of accuracy, given the variation in the experi-

Table 6: Nonlinear least-squares analysis of variance.

Source	Degrees of Freedom	Sum of Squares	Mean Square	F Value	p Value
Model	47	9.09×10^9	1.93×10^8	244	1.28×10^{-288}
Error	448	3.95×10^8	8.82×10^5		
Corrected total	495	9.49×10^9			

Table 7: Overall model fit.

Statistical metric	Value
R^2	0.925
Adjusted R^2	0.917
SSE	3.953×10^8
RMSE	939.375

345 mental data used for regression. The above statistical analysis has demonstrated
346 that the model is statistically valid, and all the fitted model parameters are sta-
347 tistically significant. This suggests that the model is not over-parametrised,
348 despite the large number of parameters.

349 The regressed model constants in Table 5 are of the same order of magnitude
350 as that reported by Shanableh (2004) who determined the kinetic parameters
351 for particulate COD degradation (both slow and fast) to be $k_0 = 9.61 \times 10^3 \text{ s}^{-1}$
352 and $E_a = 8.65 \times 10^4 \text{ J}\cdot\text{mol}^{-1}$ compared to the values regressed in this study
353 of $k_0 = 1.78 \times 10^3 \text{ s}^{-1}$ and $E_a = 4.03 \times 10^4 \text{ J}\cdot\text{mol}^{-1}$ for pCOD fast, with
354 $k_0 = 3.08 \times 10^6 \text{ s}^{-1}$ and $E_a = 1.25 \times 10^5 \text{ J}\cdot\text{mol}^{-1}$ for pCOD slow. Values of
355 the degradation of total COD from the triangular model of Li et al. (1991) in
356 Table 2 are $k_0 = 1.2 \times 10^4 \text{ s}^{-1}$ and $E_a = 6.70 \times 10^4 \text{ J}\cdot\text{mol}^{-1}$ which are also in
357 the same order of magnitude to those in the proposed model.

358 3.2. Pilot Plant Validation Study

359 To validate the proposed kinetic model, experiments were conducted on the
360 wet oxidation pilot plant described in Section 2. Experimental data from a
361 semi-batch experiment were then compared to the model predictions in Figure
362 7. It is important to note that the model used the kinetic parameters (shown in
363 Table 5) regressed from the earlier lab scale experiments and was not re-fitted
364 to the new data. The units of the gas trends plotted in Fig. 7 is the mass
365 of gas (CO_2 or O_2) remaining in the reactor at time t . Given that the pilot
366 plant did not have a stirrer, an average value of 400 for the RPM was chosen
367 although comparisons using neighbouring values of 300 and 500 showed only a
368 small degradation to the overall predictive performance.

369 There were several practical sampling problems encountered during the ex-
370 periment (which are noted in the subfigures), along with several outliers. Notwith-
371 standing, Fig. 7 shows that the model predicts the concentrations for each of the
372 measured components with a good level of accuracy. This provides confidence
373 that the model structure and specific kinetic parameters do provide an adequate
374 description of the wet oxidation of this particular organic biomass.

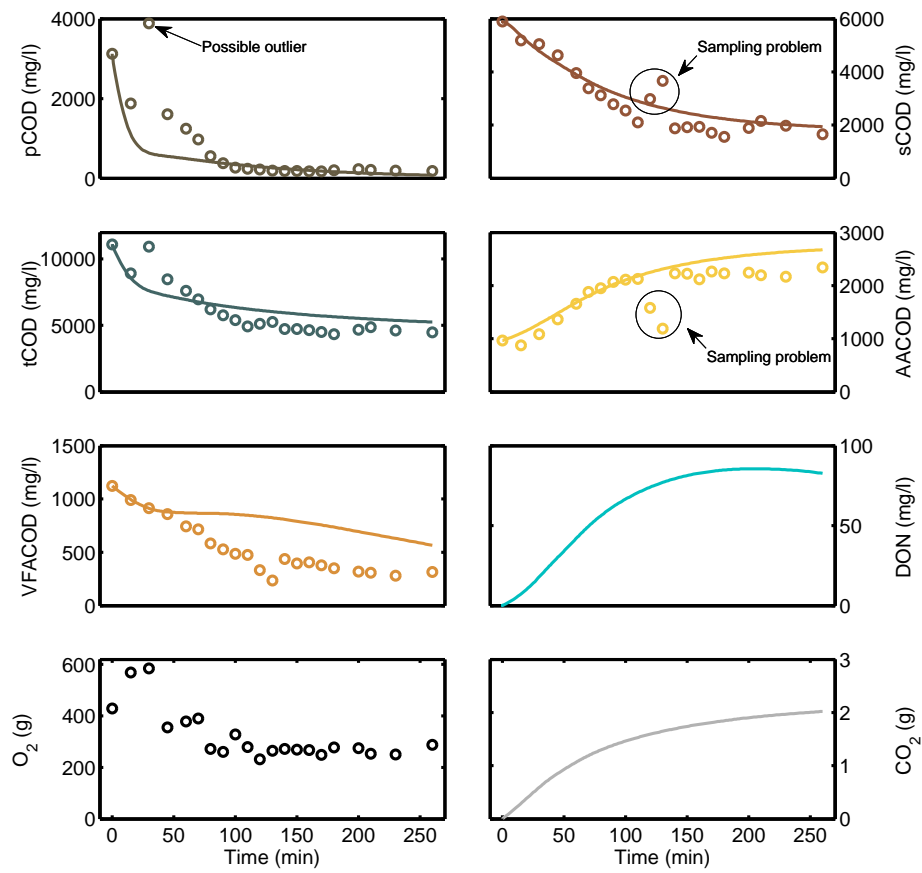


Figure 7: The kinetic model compared with a semi-batch pilot plant experiment.

375 *3.3. Establishing an Optimum Operating Point*

376 One advantage of the dynamic kinetic model developed in this study is that it
377 can be used for “what if” studies to investigate the effects of different processing
378 conditions, and in fact this was one of the primary motivations for the study.
379 For example, if the production aim was to produce both acetic acid and other
380 VFAs for use in a downstream BNR wastewater treatment plant, this would
381 require that the total VFA and acetic acid concentration is maximised. The
382 complication arises because these two components of the objective function are
383 competing.

384 Figure 8 shows the prediction of the concentration for the acetic acid, the
385 VFA and the total acetic plus VFA (in the columns) after 30 min, 1 hour and
386 2 hours (in the rows) for different operating temperatures and oxygen partial
387 pressures. Note that both the plotted temperature range (from 210°C to 260°C)
388 and the plotted oxygen partial pressure range (from 20 to 60 bar) is deliberately
389 extrapolated outside the ranges used during the experiments. (The experimen-
390 tal points for comparison are shown as the dashed rectangle in plot (g) of Fig. 8.)
391 The performance curves in Fig. 8 show that longer batch times deliver a higher
392 yield (not unexpectedly), but that the maximum is gained at lower tempera-
393 tures. The results also suggest that one should operate at low concentrations of
394 oxygen, but of course there is a limit given that there must be sufficient oxygen
395 present to prevent excessive carbon monoxide production through incomplete
396 oxidative conversion. Finally, the differences in the contour shapes at all times
397 between the acetic acid production, which favours high operating temperatures,
398 and the production of VFAs which favour low temperatures is immediately ev-
399 ident.

Figure 8: The concentration of acetic acid, VFA and the combination (in columns) as predicted from the model at different reaction times (in rows) for a range of operating temperatures and pressures. Contour lines show the concentration on a mg/L COD basis and points in plot (g) show where the experiments were undertaken.

400 This representative operation optimisation illustrates the ability of using a

401 dynamic model to highlight optimum operating points which are not always ob-
402 vious because of the requirement to maximise acetic acid and maximise VFAs
403 which are competing objectives. However it should be noted that the perfor-
404 mance in a continuous reactor may be different.

405 **4. Conclusion**

406 This paper proposes a dynamic model for wet oxidation of municipal sludge.
407 While this model is more complex than alternative models, it was shown to agree
408 closely with the concentration results obtained from the experimental investiga-
409 tion. The model contains a number of simplifications to reduce complexity and
410 the results suggest that, despite these simplifications, the model still accurately
411 captures the effects of wet oxidation. Notwithstanding, the dynamic model is
412 reasonably complex comprising of 52 parameters and a minimum of 12 dynamic
413 equations depending on the amount of experimental data. A statistical analysis
414 of the linearised model indicated that 47 fitted parameters were statistically sig-
415 nificant. The effect of temperature, oxygen partial pressure and stirring speed
416 were investigated and the effects that these parameters have on each of the
417 model components has been captured in the developed kinetic model.

418 Applying the proposed kinetic model regressed at lab-scale to subsequently
419 collected experimental data from a pilot-scale wet oxidation plant gave excellent
420 agreement across the modelled components over the environmental conditions
421 investigated. This validation step indicates that the reaction kinetics have been
422 adequately captured as part of the kinetic model and strongly suggests that the
423 model is likely to be useful at multiple scales.

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