

# **An ANN-based approach for non-destructive asphalt road density measurement**

Muyang Li<sup>1</sup>, Loulin Huang<sup>2\*</sup>, and Bryan Pidwerbesky<sup>3</sup>

<sup>1</sup>School of Engineering, Computer and Mathematical Sciences, Auckland University of Technology, 6 St Paul Street, Auckland 1010, New Zealand. Email: muyang.li@autuni.ac.nz

<sup>2</sup>School of Engineering, Computer and Mathematical Sciences, Auckland University of Technology, 6 St Paul Street, Auckland 1010, New Zealand. Email: loulin.huang@aut.ac.nz

<sup>3</sup>Fulton Hogan Ltd, 15 Sir William Pickering Drive, Christchurch 8053, New Zealand.

Email: Bryan.Pidwerbesky@fultonhogan.com

*\* Corresponding author*

## **ABSTRACT**

Asphalt pavement's density measurement is an important step in the quality control of asphalt road construction. It is usually achieved by applying the coring method (CM), nuclear density gauge (NDG), and electromagnetic density gauge (EDG). CM is the most accurate method, but it is a destructive method since the pavement is damaged when the cores are taken. NDG and EDG are non-destructive methods with high efficiency, but their measurement accuracy is poorer than that of CM. An EDG commonly used in density measurement is named pavement quality indicator (PQI). A novel method named density profiling system (DPS) is also based on the potential EDG. However, it is not applied to this research since more tests are required to verify its accuracy. This paper presents an approach to improve the accuracy of the non-destructive methods with NDG and PQI. It is based on the artificial neural network (ANN), which processes the raw data got from NDG and PQI and produces the predicted asphalt density as the output. The density measured in CM method is used as the target density and the error between ANN-predicted density and target density

24 is computed. To minimize this error, various ANN architectures and learning algorithms are tried  
25 in the ANN training process. Each established ANN model makes a substantial improvement in  
26 the performance of NDG or PQI in asphalt density measurement.

## 27 **PRACTICAL APPLICATIONS**

28 This research was initiated by Fulton Hogan (FH) Limited, a large road construction and  
29 maintenance company in New Zealand. FH lab teams are responsible for asphalt road density  
30 measurement in FH's road projects. A main method they use is to measure the densities of  
31 the cores taken from asphalt pavements (coring method). It is quite accurate but destructive  
32 and very time-consuming. They also use a nuclear density gauge (NDG) or pavement quality  
33 indicator (PQI), which are highly efficient non-destructive measurement devices. However, their  
34 measurement accuracy is poorer than that of the coring method. FH lab teams wanted to have a  
35 new density measurement method which is both accurate and efficient.

36 An ANN-based approach is presented in this paper to address the above issues faced by the FH  
37 lab teams. Densities collected with coring methods, NDG and PQI are used to train and validate  
38 the ANN models. The results from the ANNs show substantial improvements of the measurement  
39 accuracy and efficiency. The proposed approach has been presented to the FH lab teams who are  
40 impressed with its performance and plan to implement it in their projects.

## 41 **INTRODUCTION**

42 In asphalt pavement construction, it is necessary to monitor its density as an important step  
43 of quality control. A straightforward and accurate method for asphalt density measurement is the  
44 coring method (CM) (Ameri et al. 2014). In this method, asphalt core samples are extracted from  
45 the asphalt pavement by coring equipment (AS/NZS 2008). They are then transferred to a lab to  
46 be tested (AS/NZS 2014). The test procedures include the measurement of a sample's dry mass,  
47 the mass of the sample coated with a thin wax film, and the mass of the coated sample immersed  
48 into water. The so-called core density can be calculated from the mentioned three masses. The  
49 single-operator standard deviation (SD) of CM is 7.98 kg/m<sup>3</sup> while the multi-laboratory SD is

50 14.96 kg/m<sup>3</sup> (ASTM 2019). A problem with this method is that only a limited number of cores  
51 can be taken from a pavement. It is to avoid making the Swiss-cheese-like surface which is weak  
52 and unattractive. This method is hence called a destructive method. Apart from that, taking and  
53 measuring core samples and recovering the pavement are quite time-consuming and expensive.

54 More efficient measurement methods are the so-called non-destructive methods using nuclear  
55 density gauge (NDG) or electromagnetic density gauge (EDG) (Ziari et al. 2010). The working  
56 principle of the NDG is based on Compton scattering (Brisset et al. 2005). When a  $\gamma$  ray penetrates  
57 and collides with the electrons in the asphalt mixture, parts of the  $\gamma$  photons may scatter. The  
58 density is estimated from the number of scattered photons (Brisset et al. 2005; Malpass and Khosla  
59 2002). The precision of NDG is high. The single-operator SD is 25.15 kg/m<sup>3</sup> while the multi-  
60 laboratory SD is 28.03 kg/m<sup>3</sup> (ASTM 2022). However, it still cannot match that of the CM method  
61 mentioned above and has much room for improvement. In addition, nuclear radiation hazard is a  
62 big concern for its application.

63 As for EDG, a commonly used device is the pavement quality indicator (PQI) from TransTech  
64 Systems.(Ziari et al. 2010; Allen and Schultz 2003). The operational theory of PQI is based on  
65 the effects of density on the electromagnetic parameters, such as relative permittivity (dielectric  
66 constant) (Allen and Schultz 2003). A primary function of the PQI is to generate an electrical  
67 field in the asphalt pavement to manifest and measure those effects, which can be used to estimate  
68 the density through built-in algorithms (Ziari et al. 2010). According to the ASTM standard, the  
69 single-operator SD of EDG is 20.50 kg/m<sup>3</sup> while the multi-laboratory SD is 23.55 kg/m<sup>3</sup> (ASTM  
70 2016). However, due to the numerous factors (e.g., compositions, air voids, temperature) affecting  
71 the electromagnetic parameters of asphalt pavement, the actual accuracy of PQI is poorer than  
72 NDG or CM in the field measurement.

73 An up-and-coming method named density profiling system (DPS) is proposed based on ground  
74 penetrating radar (GPR), a potential EDG (Hoegh et al. 2020; Leiva et al. 2022). GPR is a prevalent  
75 device used to determine the thickness of the asphalt layer. It holds a similar operational theory  
76 to PQI, and hence it has the potential to measure the density of the asphalt pavement. In DPS,

77 3 GPRs are mounted onto a cart to measure the density continuously rather than the density of a  
78 fixed location by PQI or NDG. However, as a novel method, more tests are required to verify its  
79 accuracy. Thus, DPS is not applied in this research.

80 A common feature of non-destructive methods is that asphalt pavement's density is estimated  
81 indirectly through operational theories or empirical formulas in physics or engineering to describe  
82 the relations between the density and the nuclear or electromagnetic signals picked up directly  
83 by them. Measurement errors tend to occur from the inherent deficiency of those principles or  
84 formulas to reflect the actual relations mentioned above. Noises and factors other than the density  
85 affecting the sensors' readings also compromise the measurement accuracy.

86 Taking NDG and PQI as sensors, data processing analysis techniques for general sensors can be  
87 applied to improve their accuracy. One of the promising techniques is the artificial neural network  
88 (ANN) which is commonly used as an effective tool for processing data when the relations among  
89 the data are not easy to be established with traditional closed-form mathematical models (Bashiri  
90 and Farshbaf-Geranmayeh 2011; Tian and Shang 2006; Puig-Arnavat and Bruno 2015; Khadse  
91 et al. 2017). To mimic the biological neural system in the human body for decision-making, ANN  
92 consists of various artificial neurons organized in multiple layers (Negnevitsky 2011). Every two  
93 neurons in different layers have an internal link with a unique numerical weight, leading to the  
94 output layers where the outputs are generated. The performance of an ANN model is affected by  
95 those weights. The process to minimize the difference between the forecast output and the target  
96 is named the training process. After the training process, the optimized ANN model can then be  
97 applied to produce the output corresponding to the data collected in real time.

98 In the training process of an ANN, the weights in ANN are tuned with the learning algorithms.  
99 Three commonly used algorithms are Levenberg-Marquardt (LM), Bayesian regularization (BR),  
100 and scaled conjugate gradient (SCG) algorithms (Hagan and Menhaj 1994; Smith et al. 2019;  
101 Foresee and Hagan 1997). LM algorithm provides very efficient training for an ANN model since  
102 the second derivative computation is replaced by the approximated first derivatives computation  
103 (Hagan and Menhaj 1994). BR algorithm can improve the generation capability of an ANN model,

104 which can keep a consistence performance on different data sets (Foresee and Hagan 1997). Similar  
105 to LM algorithm, SCG algorithm can also train an ANN model efficiently by employing the first  
106 derivative computation. In addition, it uses the least computational memory than other methods  
107 (Møller 1993). The architecture of the ANN also influences its performance. For example, too  
108 many or too few neurons in the hidden layer of ANN is not recommended (Negnevitsky 2011).

109 This paper presents an ANN-based approach to improve the accuracy of the non-destructive  
110 methods (NDG and PQI) for measuring asphalt density. The readings from NDG and PQI are  
111 used as the raw data for training the ANN models. The LM, BR, and SCG algorithms are selected  
112 as learning algorithms to train the ANN models with 2 to 15 neurons in their hidden layers. The  
113 performances of the ANN models are verified by comparing them to the performances of NDG and  
114 PQI.

## 115 ASPHALT DENSITY MEASUREMENT METHODS

### 116 Coring method (CM)

117 CM is a destructive method for measuring asphalt density. It consists of two parts: core sample  
118 extraction and lab tests. Generally, at least one core sample should be extracted in each 300 m<sup>2</sup>'s  
119 area of asphalt pavement, and its location should be chosen randomly within the area (AS/NZS  
120 2008). After being extracted, it is then tested in a lab to determine the core densities using the  
121 waxing procedure (AS/NZS 2014). The dry mass of the sample is weighed primarily. The sample  
122 is then coated with a thin film of prepared wax, and the mass of the coated sample is weighed.  
123 Finally, the coated sample is immersed in water, and the mass of coated sample in water is weighed  
124 by a specific balance. The accurate core density can be calculated by using the following equation:

$$125 \quad \rho_{\text{core}} = \frac{m_1 \rho_w \rho_{\text{wax}}}{\rho_{\text{wax}}(m_2 - m_3) - \rho_w(m_2 - m_1)} \quad (1)$$

126 Where  $\rho_{\text{core}}$  is the core density of sample (kg/m<sup>3</sup>),  $\rho_{\text{wax}}$  is the density of the paraffin wax  
127 (kg/m<sup>3</sup>),  $\rho_w$  is the density of water (kg/m<sup>3</sup>),  $m_1$  is the mass in air of the dry sample (kg),  $m_2$  is the  
128 mass in air of the wax coated sample (kg),  $m_3$  is the mass in water of the wax coated sample (kg).

129 This method is considered the most accurate method for determining the asphalt pavement's  
130 density (Ameri et al. 2014). However, the obvious problem is that both two parts of this method  
131 are not efficient enough, especially for a large pavement project. Furthermore, additional workload  
132 and costs are required to recover the destroyed pavement. An inappropriate recovery of the asphalt  
133 pavement even causes a local weakness in the road and highly affects the quality of the pavement  
134 (Ziari et al. 2010).

### 135 Nuclear density gauge (NDG)

136 NDG is a standard non-destructive device for measuring the asphalt density onsite (AS/NZS  
137 2013a; AS/NZS 2013b). The field test with an NDG device is considered the most accurate  
138 non-destructive method, though its accuracy is still lower than that of CM method.

139 The operational theory of a NDG can be explained by the Compton scattering describing the  
140 interaction between a matter and the applied  $\gamma$  (gamma) rays (Brisset et al. 2005). When these  
141 rays penetrate the asphalt mixture, the  $\gamma$  photons collide with electrons presented in the measured  
142 asphalt mixture. The collisions lead to the scattering of these  $\gamma$  photons. The number of scattered  
143 photons is related to the density of measured material (Malpass and Khosla 2002). According  
144 to Beer-Lambert's law, the density of the measured material can be approximately expressed by  
145 (Laufenberg 1986):

$$146 \rho = \frac{\ln B - \ln(I_t/I_0)}{kx} \quad (2)$$

147 Where  $I_t$  is the count of transmitted photons per second after attenuation (counts/s),  $I_0$  is  
148 the count of transmitted photons per second before attenuation (counts/s),  $k$  is mass attenuation  
149 coefficient ( $\text{m}^2/\text{kg}$ ),  $\rho$  is the density of measured material ( $\text{kg}/\text{m}^3$ ),  $x$  is the thickness of the measured  
150 material (m) and  $B$  is a preset build-up factor.

151 However, the density measured by NDG is still not accurate enough compared with that mea-  
152 sured by CM (Ameri et al. 2014; Ziari et al. 2010). In addition, there are radiation hazards in NDG  
153 is a concern.

## Pavement quality indicator (PQI)

PQI is another type of device for the non-destructive measurement of asphalt density. It can also measure the air void content and the surface temperature of the asphalt mixture (Ziari et al. 2010; Allen and Schultz 2003).

A PQI contains an active region, an isolation ring, and a ground region. It measures the complex permittivity through the mentioned structure (Ziari et al. 2010; Allen and Schultz 2003; Kvasnak et al. 2007). After applying an electrical field to pure material, its complex permittivity can be gained by Debye's equation, as follows:

$$\varepsilon_r = \varepsilon_r' - j\varepsilon_r'' \quad (3)$$

$$\varepsilon_r' = \varepsilon_\infty + \frac{\varepsilon_s - \varepsilon_\infty}{1 + (f/f_r)^2} \quad (4)$$

$$\varepsilon_r'' = \frac{(\varepsilon_s - \varepsilon_\infty)f/f_r}{1 + (f/f_r)^2} \quad (5)$$

Where  $\varepsilon_s$  is the permittivity as  $f$  goes to 0 (F/m),  $\varepsilon_\infty$  is the permittivity as the frequency goes to infinity (F/m),  $f_r$  is the relaxation frequency (Hz) and  $f$  is the applied frequency (Hz). The first three terms are the properties of the material. The real part of complex permittivity is the dielectric constant which can be processed to estimate density through the built-in algorithm. The imaginary part can be converted into moisture (Kvasnak et al. 2007).

However, the asphalt mixture contains aggregate, asphalt binder, and little air. The relative permittivity of air is far lower than aggregate or binder (Porubiaková and Komačka 2015). Thus, the air void content of the asphalt mixture highly affects its complex permittivity. By the preset equations in the PQI, the measured complex permittivity is transferred to the air void content and then the density. However, asphalt mixture may also contain a little water in a wet condition. This may influence the PQI measurement since the permittivity of water is varied according to its temperature.

The models for non-destructive density measurement by NDG or PQI do not reflect all the parameters affecting the density. Their measurement accuracies are compromised and cannot match

181 the destructive method such as CM. To improve their performance, data processing techniques like  
182 ANN can be applied.

### 183 **ARTIFICIAL NEURAL NETWORK (ANN)**

184 Artificial neural network (ANN) is an efficient technique for data processing and is widely used in  
185 various applications (Bashiri and Farshbaf-Geranmayeh 2011; Tian and Shang 2006; Puig-Arnavat  
186 and Bruno 2015; Khadse et al. 2017). It has been attempted to support monitoring the quality  
187 of the asphalt pavement construction, and all applied ANN models show excellent performances  
188 (Chandrakasu et al. 2021; Commuri and Zaman 2008; Commuri et al. 2011). In this research,  
189 ANN technique is employed to improve the performance of NDG and PQI devices. The NDG-  
190 measured and PQI-measured densities are used to train the ANN models, and the ANN models  
191 output the so-called ANN-predicted densities which are then compared with the core densities.  
192 Their differences, named errors, are minimized by the ANN training process, which is guided by  
193 learning algorithms. The architecture of ANN models, training process, and learning algorithms  
194 used in this approach will be explained respectively.

### 195 **Architecture**

196 An artificial neural network is a kind of computation model inspired by the human nervous  
197 system (Negnevitsky 2011; Haykin 2000). Like the biological neural network consisting of natural  
198 neurons, ANN consists of highly interconnected units named artificial neurons, as shown in Figure  
199 1. They are connected by links passing signals from one to another. Each neuron receives input  
200 signals and the attached numerical weights through its input links. The neuron computes the  
201 weighted sum of the input signals and subsequently uses the sum to calculate the final output by  
202 an activation function. Finally, the output signal will be transmitted to other neurons as an input  
203 signal until the final output signals of the entire ANN are reached.

204 In an ANN model, artificial neurons are organized into layers. In this approach, the architecture  
205 of the ANN model is illustrated in Figure 2. It consists of an input layer, a hidden layer, and an  
206 output layer. The input layer contains two neurons which are used to pass the input data (NDG-  
207 measured and PQI-measured densities) to the neurons in the hidden layer. After the computation

208 process in each neuron, the outputs of the neurons in the hidden layer are passed to the neuron in  
209 the output layer. After the same process, the neuron in the output layer outputs the results, which  
210 are so-called ANN-predicted densities.

211 In this model, the numerical weights and the number of neurons in the hidden layer are the two  
212 essential parts required to be optimized. Their optimization processes will be introduced in the  
213 following sections.

## 214 **Training Process and Learning Algorithms**

215 The proposed ANN-based approach is illustrated schematically in Figure 3. In this research,  
216 the core densities are regarded as the target densities since they are the most accurate method to  
217 measure the density of the asphalt pavement. However, the limitation is obvious. The number of  
218 core samples that can be gained from a pavement is limited. The best way to solve this is to collect  
219 core densities from different projects containing pavements with similar conditions. The details of  
220 this part will be discussed in the next section, Data Collection.

221 As mentioned in the structure of ANN models, the NDG and PQI densities are input into the  
222 ANN models. After gaining the ANN-predicted densities, errors between them and the target  
223 densities are computed and are then used to tune the numerical weights of the ANN models. The  
224 process to search for the minimized errors and the optimized weights is named the training process.

225 Learning algorithms are employed to guide the search direction of this process. In this research,  
226 three learning algorithms are chosen, including the Levenberg-Marquardt algorithm, the Bayesian  
227 regularization algorithm, and the scaled conjugate gradient algorithm.

228 Based on the traditional Newton's method, the Levenberg-Marquardt (LM) algorithm is devel-  
229 oped to reduce the time to train an ANN model (Hagan and Menhaj 1994). In Newton's method,  
230 the search direction is determined by calculating the Hessian matrix expressed by  $\mathbf{H}_{ij} = \frac{\partial^2 F(w)}{\partial w_i \partial w_j}$  ( $i =$   
231  $1, \dots, N$ ) ( $i \neq j = 1, \dots, N$ ).  $w$  represents the weight,  $N$  represents the total number of weights and  $F$   
232 represents the objective function to be minimized. The calculation of the second derivative requires  
233 a long time and a large storage space. These problems are solved by the LM algorithm where the  
234 objective function is considered as the sum of the squared error function, which can be described

235 by  $F(w) = \sum_{i=1}^N v_i^2(w)$ . A Jacobian matrix is introduced and contains the elements  $\mathbf{J}_{ij} = \frac{\partial v_i(w)}{\partial w_j}$ .  
236 Accordingly, a Hessian matrix can be calculated approximately by  $\mathbf{H} = 2\mathbf{J}^T\mathbf{J} + 2 \sum_{i=1}^N v_i(w) \partial^2 v_i(w)$ .  
237 The later part of  $\mathbf{H}$  is commonly considered small enough and hence  $\mathbf{H} \approx 2\mathbf{J}^T\mathbf{J}$ . The Jacobian  
238 matrix only contains the first derivatives. Thus, compared with Newton's method, LM algorithm  
239 requires less time to train an ANN model.

240 The Bayesian regularization (BR) algorithm is proposed to improve the generalization capa-  
241 bilities of ANN models (Foresee and Hagan 1997). An ANN model with a good generalization  
242 capability means it performs nearly the same on both the data for training and other data. In other  
243 words, the ANN model is close to the true relationship between the input and output. With the  
244 assumption that the true relation is smooth, which corresponds to small weights in the ANN, the  
245 objective of the BR algorithm is to balance the minimization of the sum of the squared error and the  
246 sum of the weights in the ANN (Foresee and Hagan 1997; Hagan and Menhaj 1994). Hence, the  
247 BR algorithm requires more computation and is slower in training models than the LM algorithm.

248 Similar to the LM algorithm, the scaled conjugate gradient (SCG) algorithm is also proposed to  
249 train an ANN model efficiently (Møller 1993). In this algorithm, the so-called conjugate vectors,  
250 which are orthogonal to each other, are introduced. The search direction can be determined  
251 by calculating a set of conjugate vectors rather than the Hessian matrix and the Jacobin matrix.  
252 Although both a conjugate vector and the Jacobin matrix contain the first-order derivatives of the  
253 objective function, the former contains fewer elements than the latter. Thus, the SCG algorithm  
254 can train an ANN model more efficiently than LM algorithm does. In addition, less storage space  
255 is required during the training process.

256 The ANN models trained by the 3 learning algorithms are the so-called LM-ANN, BR-ANN,  
257 and SCG-ANN models, respectively. All models hold the same architecture mentioned above and  
258 will be used in the later optimization process.

## 259 DATA COLLECTION

260 To train the ANN model, a large number of data samples containing NDG, PQI, and core density  
261 are required. All data samples used in this research are collected from public data sources. The

262 main advantage of using them is to save time, which may last up to several months. However, the  
263 disadvantage is that they may contain some factors influencing the accuracy of density measurement.  
264 According to the operation theory of NDG and PQI, the factors include the aggregate types and the  
265 layer thickness of the asphalt pavement. Thus, the ideal scenario for the data collection is that all  
266 the data samples are from one pavement or several pavements with similar or the same aggregate  
267 source and layer thickness. To meet the requirement, data samples from 2 public data sources are  
268 collected and then used to train the ANN models.

269 The same data collection process is used for them. Firstly, the number of test sections and  
270 the number of core samples that will be taken in each section are calculated. Secondly, locations  
271 for taking core samples are marked and numbered. Thirdly, the NDG is placed on each marked  
272 location to measure and record density. Fourthly, the PQI is used in the same way. Finally, after  
273 NDG and PQI measurements, all the core samples are taken and sent to a lab for measuring the  
274 core densities.

275 The first data source is the field investigation taken by engineers and technicians from the North  
276 Carolina Department of Transportation (Sawyer et al. 2005). The investigation field is located on  
277 an interstate highway (I-95) in Wilson County, North Carolina. The type of asphalt mix is the  
278 Superpave Mix S-12.5D, and hence the nominal size of the aggregate is 12.5 mm. The binder  
279 grade is the PG 76-22 binder. The layer thickness is around 38 mm. 16 test sections (8 lots and 2  
280 sub-lots per lot) on the asphalt pavement are selected and the area of each one is around  $110 m^2$ . 6  
281 test locations per section are marked for conducting NDG and PQI measurements and then taking  
282 core samples. Thus, 96 data samples are collected from this data source.

283 The second one is the evaluation of the non-destructive method taken by the engineers and  
284 technicians from Kentucky Transportation Center (Allen and Schultz 2003). The evaluation field is  
285 located on another interstate highway (I-75) in Scott County, Kentucky. The same Superpave mix  
286 type (S-12.5D) and binder grade (PG 76-22) are used. 44 test sections (11 lots and 4 sub-lots per  
287 lot) on the asphalt pavements are selected. 3 or 4 locations per section are marked for conducting  
288 the same process outlined in the last data source. During the PQI measurement, 2 PQI devices are

289 employed. Their average readings are calculated and recorded as the PQI data. In this data source,  
290 143 data samples are collected.

291 Totally, 239 data samples are collected. Each data sample contains a core density, a PQI density,  
292 and an NDG density. The core density ranges from 2037 to 2485 kg/m<sup>3</sup>. The NDG density ranges  
293 from 1892 to 2465 kg/m<sup>3</sup> while the PQI density ranges from 1980 to 2502 kg/m<sup>3</sup>. The averages of  
294 the three densities are around 2311, 2271, and 2292 kg/m<sup>3</sup>, respectively. Since the core density is  
295 the target data, an NDG or PQI density is compared with the corresponding core density. The root  
296 mean squared errors (RMSEs) of NDG and PQI densities are calculated to describe their accuracies.  
297 They are 65.53 and 68.00 kg/m<sup>3</sup>, respectively. The correlations between them are described by the  
298 correlation coefficients (Rs). Figure 4 shows the data distributions and the Rs of NDG and PQI  
299 densities. The horizontal axis represents the core density. The vertical axis represents the NDG  
300 or PQI density. The Rs of NDG and PQI densities are around 0.83 and 0.87, respectively. Some  
301 outliers are clumped off the fit line, obviously. This is because the PQI and NDG measurements are  
302 inaccurate under high temperature or moisture. Data drifts may occur and lead to outliers under that  
303 condition. When many data are measured under the same condition, the outliers are then clumped  
304 off the fit line.

305 All the data samples are combined and become an original dataset for training the ANN models.

## 306 ANN MODEL'S OPTIMIZATION

307 An experiment is implemented to optimize the architecture of 3 ANN models. The numerical  
308 weights are optimized directly in the training process. The number of neurons can be optimized  
309 indirectly. In the experiment, it is preset from 2 to 15. (Negnevitsky 2011). According to the  
310 architecture of the ANN models shown in Figure 2, one neuron is not enough to handle the relations  
311 with two inputs. Hence the minimum number of neurons is 2. The maximum number of neurons  
312 is commonly set based on the performance of the models. This will be discussed later.

313 A model with each number of neurons is trained 100 times to get the average performance. The  
314 architecture of the ANN model with the best performance is the optimized one.

315 In this experiment, ANN models are created, trained, and tested by employing MATLAB,

316 which is a computational software and contains a powerful ANN toolbox. The original dataset is  
317 divided into 3 data groups, which are training, validation, and testing data groups. The training data  
318 group is directly applied for training ANN models. The validation data group is used to prevent  
319 ANN models from over-fitting and stop the training process in time. The test dataset is not used  
320 in the training process and can be used to test the accuracy and the generation capability of the  
321 ANN model. In this experiment, 60% data belongs to the training group, 20% data belongs to the  
322 validation group, and the rest 20% data belongs to the test group.

323 As shown in Table 1-3, the experimental results illustrate the performances of the 3 ANN models  
324 with different numbers of neurons in their hidden layers. In this research, the performance of an  
325 ANN contains its accuracy, generation capability, and training efficiency, which will be analyzed  
326 respectively.

### 327 **Accuracy**

328 The accuracy of each model is measured by the root mean squared error (RMSE) of its testing  
329 data group. RMSE is calculated by the following equation:

$$330 \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (X_i - Y_i)^2}{n}} \quad (6)$$

331 where  $X$  and  $Y$  are the core density and ANN-predicted density, respectively.  $n$  is the total  
332 number of densities.

333 The maximum neuron of the hidden layer is discussed. Commonly, the more neurons an ANN  
334 model holds, the more computation process it needs. It also means the more training time and space  
335 for computational storage. Thus, it is not worth having too many neurons unless the error goes  
336 down obviously with the increasing number of neurons. As shown in Figure 5, when the number  
337 of neurons increases from 10 to 15, the RMSEs of BR-ANN and SCG-ANN model keep constantly  
338 and that of LM-ANN model even slightly goes up. Thus, it is not necessary to test a model with  
339 more than 15 neurons.

340 In addition, as shown in Figure 5, the BR-ANN model holds the least RMSE among all three

341 models. Obviously, the BR-ANN model holds a low RMSE when there are 4 or 10 neurons in its  
342 hidden layer. The two RMSEs are 27.29 and 27.67 kg/m<sup>3</sup>, respectively. They are very close. The  
343 LM-ANN model holds the second least RMSE. As the number of neurons goes up from 2 to 4,  
344 the RMSE of the LM-ANN model goes down. On the other hand, as the number of neurons goes  
345 up from 4 to 15, its RMSE goes up. Thus, an optimized architecture of the LM-ANN model is  
346 that it holds 4 neurons in its hidden layer. The SCG-ANN model holds the largest RMSE, and the  
347 SCG-ANN model with 8 neurons is an optimized architecture.

### 348 **Generalization capability**

349 The generation capability of an ANN model is measured through the difference between the  
350 RMSEs of the training, validation, and testing data groups. As shown in Figure 6, as the number of  
351 neurons goes up, the generation capability of LM-ANN model becomes worse and worse. To gain  
352 a reasonable generation capability, the number of neurons in the hidden layer should be less than  
353 5. As shown in Figure 7, the BR-ANN model illustrates an excellent generation capability since  
354 the RMSEs of all data groups are close to each other. The number of neurons in its hidden layer  
355 does not affect its generation capability. As shown in Figure 8, the SCG-ANN model also shows  
356 an excellent generation capability. When the number of neurons is more than 10, the difference  
357 between the RMSEs of the training group and the validation group becomes larger. Hence, in terms  
358 of the SCG-ANN model, the number of neurons in its hidden layer should be less than 10.

### 359 **Training efficiency**

360 The training efficiency of a learning algorithm is measured by the length of time for training an  
361 ANN model. As shown in Figure 9, The SCG algorithm is the most efficient for training the ANN  
362 model. The training time of SCG-ANN model is stable, which means it is not influenced by the  
363 number of neurons. The LM algorithm shows a similar training efficiency to the SCG algorithm  
364 when there are more than 3 neurons in the hidden layer of the trained model. The BR algorithm  
365 requires the longest time to train an ANN model. The training time becomes longer and longer  
366 when the number of neurons goes up. Thus, a BR-ANN model with 4 neurons in its hidden layer  
367 can be trained more efficiently than the one with 10 neurons in its hidden layer.

368 By comparing all three aspects of their performances, the optimized architectures of the 3  
369 models are the LM-ANN model with 4 neurons, the BR-ANN model with 4 neurons, and the  
370 SCG-ANN model with 8 neurons in their hidden layers respectively.

## ANN MODEL'S EVALUATION AND DISCUSSION

### RMSE and the precision of measurement

There is no direct relationship between RMSE and the ASTM/AASHTO reported precision. According to the ASTM and AASHTO standards, the precision of NDG or PQI measurement is indicated by the standard deviation (SD) (ASTM 2022; ASTM 2016; AASHTO 2022). It measures the average variability of a kind of density. On the other hand, RMSE measures the difference between core and other densities. However, RMSE and SD have an indirect relation in this research. A lower RMSE means that the corresponding density is closer to the core density. It also means that the SD of the corresponding density becomes lower as the core density holds the lowest SD. Thus, if the ANN-predicted density holds a lower RMSE than that of NDG or PQI density, it means that the ANN model produces a density with a higher precision than the one measured by NDG or PQI.

As can be seen in Table 4, The RMSEs of the ANN-predicted densities are around 30 kg/m<sup>3</sup>. On the contrary, the RMSEs of the NDG and PQI densities are both more than 60 kg/m<sup>3</sup>, which is far more than the RMSEs of the ANN-predicted densities. Thus, the precision of the NDG or PQI density is improved greatly by employing the ANN models to predict the density.

### Correlation coefficient (R)

Correlation coefficients (Rs) are employed to indicate the closeness of the ANN-predicted densities to the core densities. The following equation calculates R:

$$R = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2 (Y_i - \bar{Y})^2}} \quad (7)$$

where  $X_i$  and  $Y_i$  are the core density and ANN-predicted density, respectively.  $\bar{X}$  and  $\bar{Y}$  are the average values of  $X_i$  and  $Y_i$ , respectively.  $n$  is the total number of densities.

As mentioned in the previous section, Figure 4 shows the original performance of NDG and PQI without the assistance of the ANN models. The Rs of NDG and PQI densities are around 0.83 and 0.87, respectively.

396 Figure 10 - 12 show the performance of the 3 ANN models with their optimized architectures.  
397 Each figure contains four graphs representing the performances of the training, validation, and  
398 testing data groups and the overall performance, respectively. The LM-ANN model holds the best  
399 overall performance ( $R \approx 0.94$ ) among all the models. However, the BR-ANN model holds the  
400 best performance of its testing data group ( $R \approx 0.94$ ). In addition, the BR-ANN model has the  
401 best generation capability since its 3 data groups hold a similar R (around 0.94, 0.95, and 0.94,  
402 respectively). The generation capability of the SCG-ANN model is also reasonable, although it  
403 holds the worst performance ( $R \approx 0.92$ ).

404 As for the data distribution associated with the LM-ANN and BR-ANN models, there are not  
405 too many clumped outliers and most of the data points are close to the fit line, which leads to high  
406 R values. Thus, the models are close to the true relation. On the other hand, the SCG-ANN model  
407 produces some clumped outliers. The reason can be that the search direction of the SCG algorithm  
408 requires conjugate vectors, which contain less information than the Jacobian matrix required by that  
409 of the LM and BR algorithms. Hence, the relation searched by the SCG algorithm is commonly  
410 worse than that of the LM or BR algorithm.

411 Since each of the ANN models has a higher R-value than that of NDG or PQI, the ANN models  
412 are verified to improve the performance of NDG and PQI greatly. However, some outliers still  
413 exist. The reason may be that some input densities contain large drifts or errors and many of them  
414 are allocated to the training groups.

## 415 **CONCLUSION**

416 This paper presents an ANN-based approach to improve the accuracy of asphalt density measure-  
417 ment with non-destructive methods such as NDG and PQI. The NDG-measured and PQI-measured  
418 densities are used as the inputs of the ANN models while the core densities are used as the target  
419 (desired) densities. Three learning algorithms, LM, BR, and SCG algorithms are applied to train  
420 the ANN models, and their performances are compared and the ANN architectures are optimized  
421 accordingly. It is shown that the proposed approach improves the accuracy of the non-destructive  
422 methods significantly. The next step is to collect additional data to train the proposed models con-  
423 tinuously. The density from the pavements with a similar pavement thickness is helpful in further  
424 improving the accuracy of the data. The additional data can be directly combined with the current  
425 data samples since more data improves the ability of ANN models to filter noise and the outlier.  
426 Data containing temperature and moisture may also be helpful. The density from the pavement  
427 with a thinner or thicker layer may be helpful to improve the generation capabilities of the models.

428 **DATA AVAILABILITY STATEMENT**

429 All the data that support the findings of this study are from public data sources. All models,  
430 or code that support the findings of this study are available from the corresponding author upon  
431 reasonable request.

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**TABLE 1.** The performance of the LM-ANN model with different numbers of neurons in its hidden layer

The number of neurons in the hidden layer	LM-ANN model			
	Training time (s)	RMSE (kg/m <sup>3</sup> )		
		Training	Validation	Testing
2	0.15	29.53	29.48	30.61
3	0.08	27.79	28.89	29.01
4	0.08	26.50	27.42	28.63
5	0.08	25.52	27.01	28.90
6	0.07	25.44	27.38	30.39
7	0.07	25.43	27.85	30.82
8	0.07	24.93	28.74	31.57
9	0.07	25.11	28.33	30.14
10	0.08	24.66	28.92	31.37
11	0.07	24.61	28.09	30.01
12	0.07	24.65	28.33	30.78
13	0.07	24.33	28.71	31.94
14	0.08	24.24	29.21	31.21
15	0.07	25.46	31.29	32.03

**TABLE 2.** The performance of the BR-ANN model with different numbers of neurons in its hidden layer

The number of neurons in the hidden layer	BR-ANN model			
	Training time (s)	RMSE (kg/m <sup>3</sup> )		
		Training	Validation	Testing
2	0.09	27.23	27.44	28.23
3	0.09	26.69	27.29	28.16
4	0.10	26.40	27.24	27.29
5	0.10	26.55	27.52	27.87
6	0.11	26.44	26.92	28.04
7	0.10	27.16	27.78	28.16
8	0.10	26.74	28.04	28.93
9	0.10	27.79	28.33	29.41
10	0.12	26.92	27.56	27.67
11	0.11	27.26	28.28	28.52
12	0.11	26.83	27.92	28.09
13	0.11	26.42	27.77	28.45
14	0.13	26.44	27.43	28.03
15	0.11	27.11	28.41	28.88

**TABLE 3.** The performance of the SCG-ANN model with different numbers of neurons in its hidden layer

The number of neurons in the hidden layer	SCG-ANN model			
	Training time (s)	RMSE (kg/m <sup>3</sup> )		
		Training	Validation	Testing
2	0.08	33.47	33.54	35.35
3	0.07	32.94	32.73	33.74
4	0.07	32.34	32.19	33.40
5	0.07	32.26	31.91	33.45
6	0.07	31.82	32.13	33.05
7	0.07	31.74	31.18	33.39
8	0.07	30.77	30.55	31.80
9	0.07	30.76	30.92	33.03
10	0.07	30.97	30.49	32.27
11	0.07	30.61	29.71	33.37
12	0.07	30.21	30.98	32.51
13	0.06	29.52	31.58	32.62
14	0.07	29.70	31.31	32.42
15	0.07	30.12	30.46	33.09

**TABLE 4.** The RMSEs of the ANN-predicted densities and the measured densities.

ANN-Predicted Densities			NDG	PQI
LM-ANN model	BR-ANN model	SCG-ANN model	Density	Density
28.63	27.29	31.08	65.53	68.00