



# Inverse MultiView. II. Microarcsecond Trigonometric Parallaxes for Southern Hemisphere 6.7 GHz Methanol Masers G232.62+00.99 and G323.74–00.26

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Received 2022 December 7; revised 2023 May 15; accepted 2023 May 16; published 2023 July 28

## Abstract

We present the first results from the Southern Hemisphere Parallax Interferometric Radio Astrometry Legacy Survey: 10  $\mu$ as accurate parallaxes and proper motions for two Southern Hemisphere 6.7 GHz methanol masers obtained using the inverse MultiView calibration method. Using an array of radio telescopes in Australia and New Zealand, we measured trigonometric parallaxes and proper motions for the masers associated with the star formation region G232.62+00.99 of  $\pi = 0.610 \pm 0.011$  mas,  $\mu_x = -2.266 \pm 0.021$  mas yr<sup>-1</sup>, and  $\mu_y = 2.249 \pm 0.049$  mas yr<sup>-1</sup>, which implies its distance to be  $d = 1.637 \pm 0.029$  kpc. These measurements represent an improvement in accuracy by more than a factor of 3 over the previous measurements obtained through Very Long Baseline Array observations of the 12 GHz methanol masers associated with this region. We also measure the trigonometric parallax and proper motion for G323.74–00.26 as  $\pi = 0.364 \pm 0.009$  mas,  $\mu_x = -3.239 \pm 0.025$  mas yr<sup>-1</sup>, and  $\mu_y = -3.976 \pm 0.039$  mas yr<sup>-1</sup>, which implies a distance of  $d = 2.747 \pm 0.068$  kpc. These are the most accurate measurements of trigonometric parallax obtained for 6.7 GHz class II methanol masers to date. We confirm that G232.62+00.99 is in the Local Arm and find that G323.74–00.26 is in the Scutum–Centaurus arm. We also investigate the structure and internal dynamics of both masers.

*Unified Astronomy Thesaurus concepts:* [Astrophysical masers \(103\)](#); [Radio astrometry \(1337\)](#); [Very long baseline interferometry \(1769\)](#)

*Supporting material:* data behind figures

## 1. Introduction

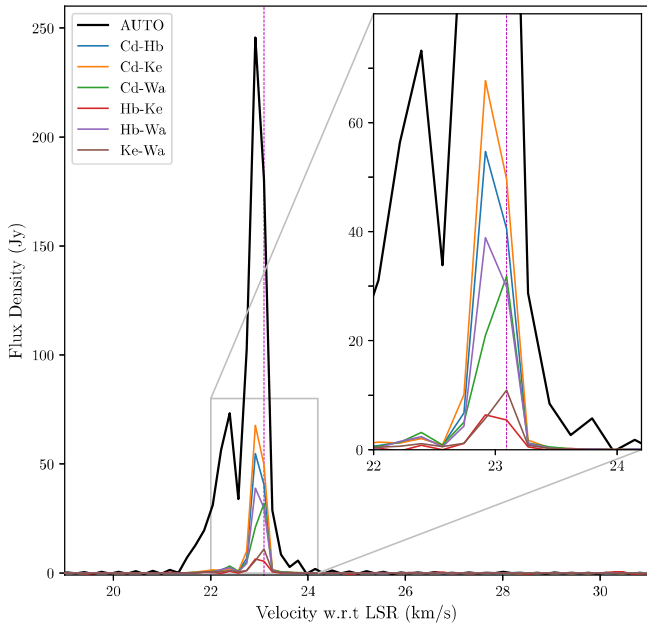
Measuring the trigonometric parallax (hereafter “parallax”) and proper motion of stars or star-forming regions that trace the motion of interstellar gas is the best method to accurately determine the structure and kinematics of the Milky Way. Parallax measurements at radio frequencies have the advantage of not being obscured by dust and can therefore probe much deeper into the disk of the Galaxy than those at optical frequencies.

Very long baseline interferometry (VLBI) has been demonstrated to be able to achieve parallax accuracies of  $\pm 10$   $\mu$ as and therefore measure objects at a distance of 10 kpc with 10% accuracy (Reid & Honma 2014). Thus far, this level of accuracy has been almost exclusively achieved at radio frequencies above 10 GHz and with homogeneous telescope arrays (e.g., the Very Long Baseline Array, VLBA). At lower frequencies, uncompensated dispersive delays from the ionosphere can cause large systematic and direction-dependent errors (Reid et al. 2017; Rioja et al. 2017; Rioja & Dodson 2020).

MultiView (hereafter “direct MV”; Rioja et al. 2017) has been shown to give astrometric accuracies approaching values determined by the thermal noise. A new variation called inverse MultiView (iMV) has recently been developed that allows additional robust calibration of short-timescale quasi-random phase changes at the position of that target for target-calibrator separations of up to 7° at 8.3 GHz (Hyland et al. 2022).

The Southern Hemisphere Parallax Interferometric Radio Astrometry Legacy Survey (S $\pi$ RALS; Hyland 2021) is an extension of the Bar and Spiral Structure Legacy Survey (BeSSeL; Reid et al. 2009b; Brunthaler et al. 2011; Reid et al. 2014, 2019) and VLBI Exploration of Radio Astrometry (VERA; VERA Collaboration et al. 2020), with the aim to obtain information on the structure of the Milky Way for those regions exclusively visible from the Southern Hemisphere. The S $\pi$ RALS targets 6.7 GHz methanol masers (Menten 1991), which are known to exclusively trace high-mass star formation (Minier et al. 2001; Ellingsen 2007; Breen et al. 2013). At these relatively low frequencies, the iMV approach can greatly improve the calibration of the dispersive delays due to the ionosphere.

In this paper, we demonstrate the calibration capabilities of iMV by measuring 10  $\mu$ as accurate parallaxes of two 6.7 GHz methanol masers. In Section 2, we describe the target and calibrator selection and observations. In Section 3, we outline



**Figure 1.** Auto- and cross-correlated spectra of G232.62+00.99 maser emission at epoch 6. The autocorrelated peak flux density (black line), is  $\sim 250$  Jy, and the Ke–Wa (the longest baseline) cross-correlated peak flux density is 10 Jy. The reference feature at  $23.08 \text{ km s}^{-1}$  is indicated by the vertical dashed magenta line.

(The data used to create this figure are available.)

all data reduction and analysis, including iMV calibration and parallax fitting. Section 4 presents the results, and Section 5 includes a discussion of our findings.

## 2. Methods

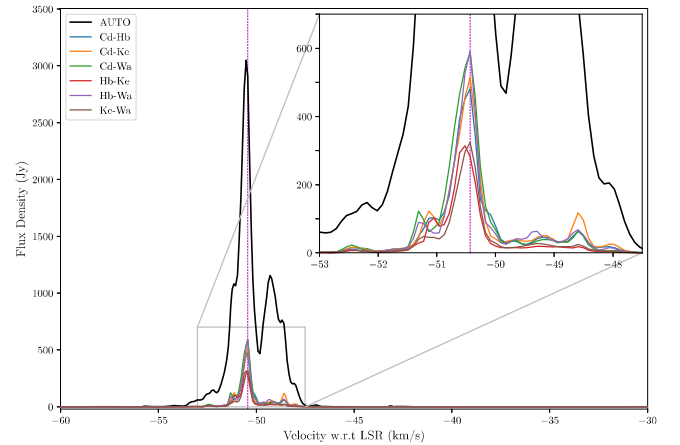
### 2.1. Source Selection and Observations

We selected two class II 6.7 GHz masers from the Methanol Multibeam Catalogue (Caswell et al. 2010, 2011; Green et al. 2012; Breen et al. 2015) that our pilot observations revealed to have compact emission in at least one  $2 \text{ kHz}/0.087 \text{ km s}^{-1}$  velocity channel. The first was G232.62+00.99 (MacLeod et al. 1992), a maser associated with the H II region RCW 7 (Dubout-Crillon 1976). As this target is at a decl. of  $-17^\circ$ , it is visible from both the Northern and Southern Hemispheres. Consequently, this maser region had an existing parallax measurement from the BeSSeL project (at 12 GHz; Reid et al. 2009a). This allows a direct comparison of parallaxes measured by the BeSSeL survey and  $S\pi$  RALS.

The second maser was G323.74–00.26 (MacLeod et al. 1992), one of the strongest 6.7 GHz methanol masers known, which has been exhibiting a peak flux density of over 3000 Jy (while flares with a flux density of up to 5800 Jy have also been observed; Goedhart et al. 2004). This maser is at a decl. of  $-56^\circ$  and hence only visible to Southern Hemisphere instruments. There have been numerous studies of the 6.7 GHz methanol maser emission associated with this region (Norris et al. 1993, 1998; Phillips et al. 1998; Walsh et al. 2002; Ellingsen 2007; Vlemmings et al. 2011).

The spectra of G232.62+00.99 and G323.74–00.26 as detected by our array are shown in Figures 1 and 2, respectively.

Hyland et al. (2022) showed that iMV with calibrators up to  $\approx 7^\circ$  separation from the target source can be successful at



**Figure 2.** Auto- and cross-correlated spectra of G323.74–00.26 maser emission at epoch 4. The autocorrelated peak flux density is  $\sim 3500$  Jy, and the Ke–Wa cross-correlated flux density (brown line) peaks at 300 Jy at a velocity of  $-50.52 \text{ km s}^{-1}$  (indicated by the vertical dashed magenta line).

(The data used to create this figure are available.)

8.3 GHz. At the lower frequency of 6.7 GHz, we chose calibrators separated by up to  $5^\circ.5$ . Allowing calibrators that are located up to this radius from a target provides many more bright and compact sources compared to the limitation that is usually applied for standard phase-referenced astrometric observations ( $< 2^\circ$ ).

Therefore, for both of the target masers, we selected calibrators that met the following criteria (in order of priority):

1. unresolved flux density  $> 100 \text{ mJy}$ ;
2. within  $5.5^\circ$  separation; and
3. uniform directional sky sampling (with the target near the center).

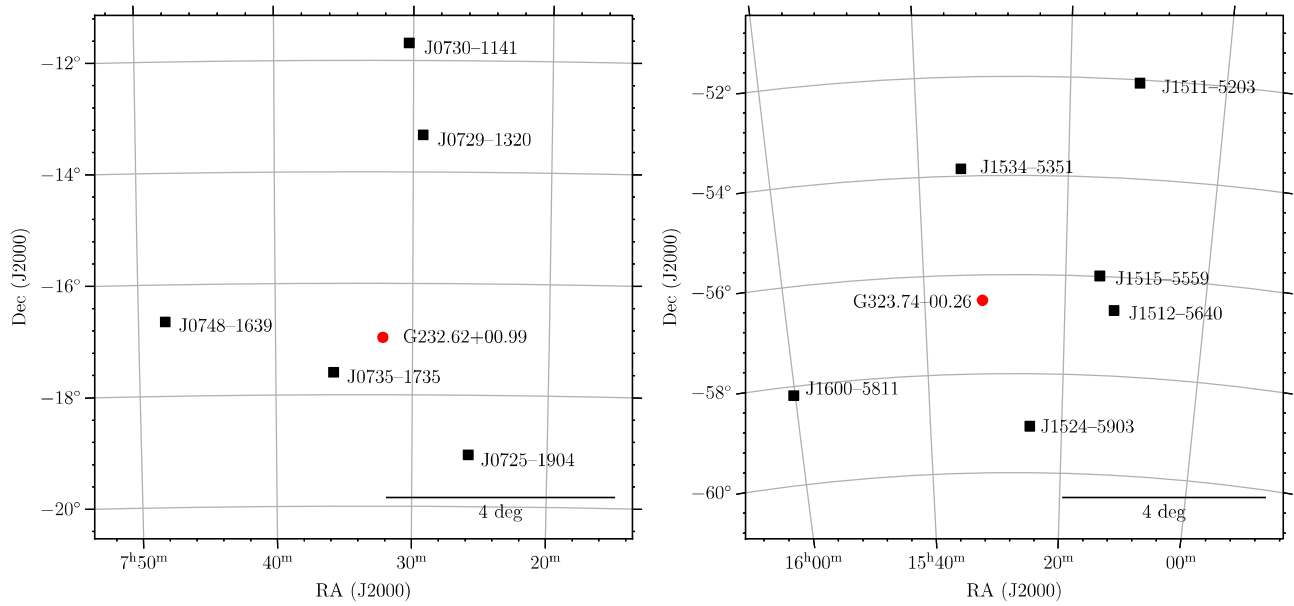
For G232.62+00.99, we chose four calibrators separated by between  $1^\circ$  and  $4^\circ$  from the target (Table 1), originally from the catalog of Petrov et al. (2019). The fifth quasar, at an angular separation of  $5.3^\circ$  (J0730–1141), was chosen as an electronic or “manual-phase” calibrator; however, its proximity to the target allowed incorporation into the iMV cycle.

For G323.74–00.26, we inferred the 6.7 GHz flux densities of the calibrators from the available 8 GHz data (Petrov et al. 2019). Using the selection criteria above, we chose the six calibrators listed in Table 1. Note that there were no good<sup>9</sup> calibrators known within  $2^\circ$  of G323.74–00.26; therefore, standard phase referencing would have been difficult and likely to produce poor astrometric results.

The distribution of the calibrators around the targets is shown in Figure 3, and Table 1 contains the calibrator positions and flux densities listed in the order they were observed when nodding between the target and calibrator.

The structure of an individual observation session of 9 hr was almost identical to that used by Hyland et al. (2022), with direct MV blocks bracketed by “geodetic-like” calibration blocks (Honma et al. 2007; Reid et al. 2009a; Reid & Honma 2014) and scans on bright compact calibrators. We observed seven epochs over a period of 1.5 yr for G232.62

<sup>9</sup> Those exhibiting a flux density greater than 100 mJy, with positions known to better than 0.3 mas and/or with little to no extended structure.



**Figure 3.** Sky distributions of target masers (red dot) and calibrators (black squares). Left: target maser G232.62+00.99 with five calibrator QSOs. The smallest calibrator separation is  $1.06^\circ$  (J0735–1735), and the largest is  $5.30^\circ$  (J1730–1141). Right: target maser G323.740–0.263 with six calibrator QSOs. The smallest calibrator separation is  $2.36^\circ$  (J1515–5559), and the largest is  $5.37^\circ$  (J1511–5203).

**Table 1**  
Target Maser and Calibrator QSO Correlated Positions, Angular Separations, and Flux Densities

Source Name		R.A. (J2000) h m s (3)	Decl. (J2000) deg arcmin arcsec (4)	Separation			Flux Density (Jy) (8)
Target Maser (1)	Calibrator QSOs (2)			$\Delta\alpha \cos \delta_r$ (deg) (5)	$\Delta\delta$ (deg) (6)	$\theta_{\text{sep}}$ (deg) (7)	
G232.62+00.99		07 32 09.78	−16 58 12.80				$\sim 10^a$
	J0735–1735	07 35 45.812460	−17 35 48.50242	0.86	−0.62	1.06	0.10
	J0725–1904	07 25 50.165557	−19 04 19.07419	−1.51	−2.10	2.58	0.15
	J0729–1320	07 29 17.817692	−13 20 02.27125	−0.68	3.64	3.70	0.12
	J0748–1639	07 48 03.083813	−16 39 50.25355	3.80	0.31	3.81	0.30
	J0730–1141	07 30 19.112473	−11 41 12.60061	−0.44	5.28	5.30	3.18
G323.74−00.26		15 31 45.45	−56 30 50.10				$\sim 300^b$
	J1534–5351	15 34 20.660723	−53 51 13.42272	0.36	2.66	2.68	0.13 <sup>c</sup>
	J1600–5811	16 00 12.377460	−58 11 02.96855	3.92	−1.67	4.18	0.32 <sup>c</sup>
	J1524–5903	15 24 51.122912	−59 03 39.71702	−0.95	−2.55	2.71	0.06 <sup>c</sup>
	J1512–5640	15 12 55.819395	−56 40 30.64300	−2.60	−0.16	2.60	0.20 <sup>c</sup>
	J1515–5559	15 15 12.672909	−55 59 32.83823	−2.28	0.52	2.36	0.26 <sup>c</sup>
J1511–5203	15 11 08.926191	−52 03 47.25032	−2.84	4.45	5.37	0.05 <sup>c</sup>	

**Notes.** The QSOs are ordered in the sequence that they were observed. Columns (1) and (2): target maser and calibrator QSO name. Columns (3) and (4): R.A. and decl. position. Columns (5) and (6): angular separation in R.A. and decl. Column (7): total separation. Column (8): flux density.

<sup>a</sup> Correlated flux density of  $+23.09 \text{ km s}^{-1}$  channel at epoch 6 on Ke–Wa baseline ( $\sim 4750 \text{ km}$ ).

<sup>b</sup> Correlated flux density of  $-50.52 \text{ km s}^{-1}$  channel at epoch 4 on Ke–Wa baseline ( $\sim 4750 \text{ km}$ ).

<sup>c</sup> Cataloged unresolved flux density at 8.4 GHz.

+00.99 and seven epochs spanning 1 yr for G323.74−00.26. The dates of the observations were chosen to sample near the extremes of the parallax oscillation in R.A. in order to optimize the accuracy to which the observations can measure the parallax. We refer to these maxima as “parallax seasons.”

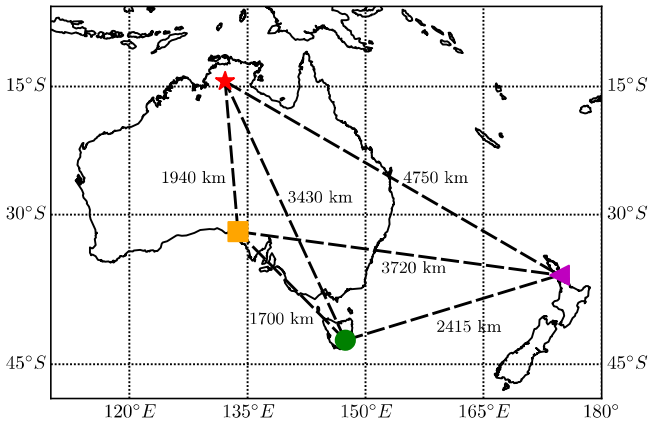
## 2.2. Array, Frequency, and Correlation

The array used for these observations is shown in Figure 4, comprising the University of Tasmania telescopes Ceduna 30 m (Cd; McCulloch et al. 2005), Hobart 12 m (Hb), and Katherine 12 m (Ke; Lovell et al. 2013) and the Auckland

University of Technology telescope Warkworth 30 m (Wa; Woodburn et al. 2015). This array has a maximum baseline length of 4750 km.

We recorded data at 1024 Mbps in dual polarization, Nyquist sampled at  $2 \text{ bits sample}^{-1}$ , over the frequency range 6580–6708 GHz. The Cd and Wa antennas recorded right and left ( $\mathcal{R}, \mathcal{L}$ ) circular polarizations, while Hb and Ke recorded horizontal and vertical ( $\mathcal{H}, \mathcal{V}$ ) linear polarizations.

Baseband data were correlated using DiFX-2 (Deller et al. 2011) in two passes; all sources were correlated over the full recorded frequency range with 0.5 MHz frequency channels, and the iMV blocks were correlated in a 4 MHz “zoom” band



**Figure 4.** The VLBI array used for these observations, with Cd (orange square), Hb (green circle), Ke (red star), and Wa (purple triangle). Baselines are indicated with dashed-dotted lines, and baseline lengths are given next to the corresponding baselines.

approximately centered on the frequency of the maser emission. The zoom band data for G232.62+00.99 were correlated to give frequency channels of 4 kHz, corresponding to velocity channels of  $0.174 \text{ km s}^{-1}$ ; for G23.74-00.26, we used frequency channels of 2 kHz giving velocity channels of  $0.087 \text{ km s}^{-1}$ .

In order to create valid FITS files from our mixed polarization (i.e.,  $\mathcal{HR}$ ,  $\mathcal{VR}$ ,  $\mathcal{HL}$ ,  $\mathcal{VL}$ ,  $\mathcal{RR}$ ,  $\mathcal{LL}$ ,  $\mathcal{RL}$ , and  $\mathcal{LR}$ ) data (in *difx2fits*), we treated Hb and Ke  $\mathcal{H}$  as  $\mathcal{R}$  and  $\mathcal{V}$  as  $\mathcal{L}$  in our correlation. This approach was required because we were unsuccessful at converting the mixed polarization products to a pure circular basis owing to a lack of understanding of the complex apparent feed rotation characteristics of the Wa (see Section 3.2). This would reduce the amplitudes of the mixed polarization products by  $\sqrt{2}$  (for an unpolarized source). Methanol masers at 6.7 GHz are known to exhibit low linear (typically 1.0%–2.5%, maximum 17%) and circular (typically 0.5%–0.75%, maximum 6%; Surcis et al. 2022) polarization. The visibility amplitudes of the mixed products on both masers do not differ by more than 20%, where we attribute most of this to a lack of exact amplitude and/or polarization calibration (e.g., Dodson 2008). In either case, we did not see any obvious adverse effects on our astrometric accuracy.

### 3. Data Reduction and Analysis

#### 3.1. Preliminary Reduction

We calibrated the correlated data in a similar manner to Hyland et al. (2022), with a few changes to account for dual polarization/spectral line data and that the targets may have significant positional changes over the year(s). Briefly, using *AIPS*/ParselTongue (Greisen 1990, 2003; Kettenis et al. 2006), the additional steps to calibrate the data were as follows:

1. Apparent feed rotation corrections were applied to the dual polarization data with task CLCOR/PANG (see Section 3.2 for a detailed discussion of the complex correction needed for the Wa antenna).
2. Source position shifts (to improve the relative positions among the sources) were applied with task CLCAL/ANTP.
3. Tasks SETJY/CVEL were used to correct for the Earth’s (rotation and orbital) Doppler shift, ensuring that the

maser spectra were aligned in frequency during and across epochs.

4. A maser channel was selected to be the phase reference, and the task FRING was used to solve for the phase and rate on that single channel. The criterion for channel selection was the maximum flux density on the long Ke–Wa baseline.
5. The visibilities for the continuum sources were averaged in frequency using the task SPLIT, and then the phases and rates from the maser reference channel were applied.
6. The calibrators were imaged using the IMAGR task. The position offset was determined for each calibrator, and the weighted offsets of all calibrators were assumed to reflect a position error in the reference maser spot. The maser position corrections were measured for each observing season ( $x_T$ ,  $y_T$ ). Individual calibrator source offsets were used to refine their positions relative to the new maser position at one epoch. All position offsets were applied to each source in step 2. It is important to note that the final calibrator positions were required to be consistent for all epochs.
7. The calibrators were averaged in frequency using the task SPLAT, and the phase was measured with the CALIB task. The solutions were output and used for iMV fitting (described in Section 3.3).

#### 3.2. Wa Apparent Feed Rotation Correction

The Wa antenna is a Nasmyth wheel-on-track antenna with a beam waveguide design (Petrov et al. 2015). The physical feed does not rotate when the antenna moves, and a system of four mirrors directs the beam into the receiver, i.e., a beam waveguide system, which is not uncommon for converted telecom antennas (Warkworth NZ, Yamaguchi JP, Nkutunse GH, etc). At the time of analysis, the standard *AIPS* task CLCOR/PANG did not include corrections for this type of focus. In order to combine the dual polarization data, we needed to correct for the phase introduced as the antenna moves in azimuth and elevation.

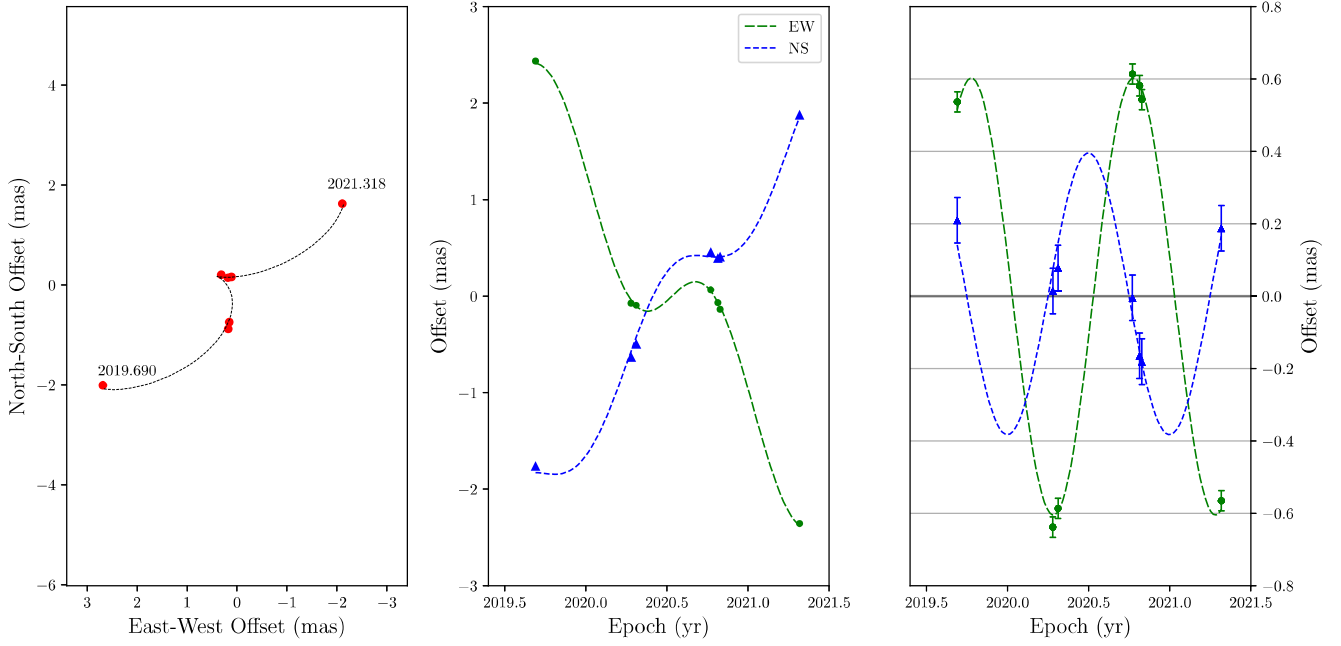
We found that the phase correction,  $\varphi$ , that accounts for the apparent feed rotation is

$$\varphi = -q - \mathcal{A} + \mathcal{E}, \quad (1)$$

where  $q$  is the parallactic angle,  $\mathcal{A}$  is the azimuth angle (measured north through east), and  $\mathcal{E}$  is the elevation angle. Subtracting  $\varphi$  from the right circularly polarized signal ( $\mathcal{R}$ ) and adding it to the left circularly polarized signal ( $\mathcal{L}$ ) phase corrects the visibility data for the apparent feed rotation, allowing the  $\mathcal{R}$  and  $\mathcal{L}$  data to be averaged before fringe fitting on the maser and increasing the signal-to-noise ratio by a factor of  $\sqrt{2}$ . The feed correction has subsequently been added to the CLCOR task, and the technical details are described in Dodson & Rioja (2022).

#### 3.3. iMV Calibration

Given the existence of occasional phase wraps in the 8.3 GHz experiments described by Hyland et al. (2022), we expected a similar or greater number to be present at 6.7 GHz. The residual path delay,  $\Delta\tau$ , for a dispersive medium like the ionosphere scales with frequency,  $\nu$ , as  $\nu^{-2}$ . The interferometer phase,  $\phi$ , is given by  $\phi = \Delta\tau\nu$ ; thus, the effect on the phase scales as  $\nu^{-1}$ . Therefore, scaling from 8.3 to 6.7 GHz should



**Figure 5.** Parallax and proper-motion modeling of the G232.62+00.99 velocity channel  $v = 23.08 \text{ km s}^{-1}$ . Left: total sky position change over the full observation period. Middle: decomposition of sky motion into east–west (green dotted–dashed line) and north–south (blue dashed line) motion over time. Right: proper-motion-subtracted sky motion over time. Error bars include  $1\sigma$  error floors for each coordinate of 28 and  $62 \mu\text{s}$  for the east–west and north–south directions, respectively.

**Table 2**  
Epochs of VLBI Observations and Astrometric Positions

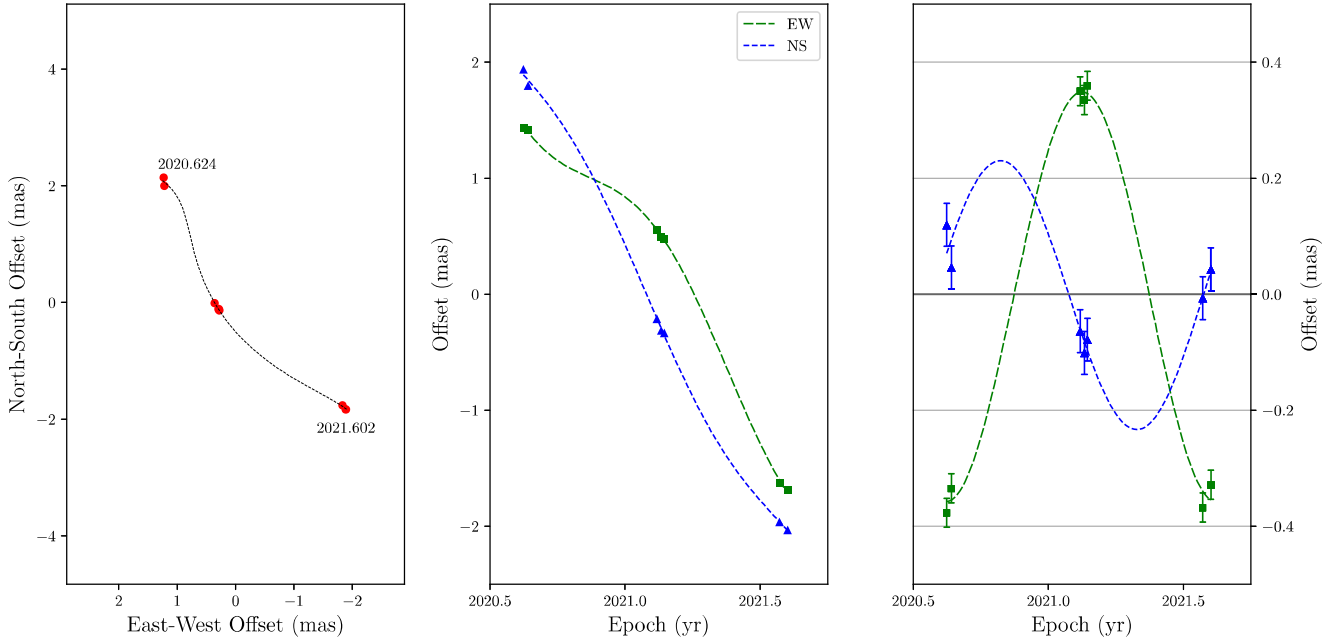
Target	Epoch	Date	Target Shift		w.r.t. Ref. Pos.		Meas. Offset		Total Offset	
			$x_T$ $x_{\text{tot}}$ (mas)	$y_T$ $y_{\text{tot}}$ (mas)	$x_T - \tilde{x}_T$ (mas)	$y_T - \tilde{y}_T$ (mas)	(mas)	(mas)	(mas)	(mas)
G232.62+00.99	1	2019 Sep 09	20.82	242.083	2.7	−2.2	−0.028	0.177	2.692	−2.023
	2	2020 Apr 12	18.42	243.583	0.3	−0.7	−0.146	−0.203	0.154	−0.903
	3	2020 Apr 24	18.42	243.583	0.3	−0.7	−0.212	−0.263	0.088	−0.963
	4	2020 Oct 09	18.22	244.383	0.1	0.1	0.208	0.110	0.308	0.210
	5	2020 Oct 25	18.22	244.383	0.1	0.1	−0.009	0.093	0.091	0.193
	6	2020 Oct 30	18.22	244.383	0.1	0.1	−0.043	0.063	0.057	0.163
	7	2021 Apr 26	16.22	245.883	−1.9	1.6	−0.203	−0.017	−2.103	1.583
		Ref. pos. ( $\tilde{x}_T, \tilde{y}_T$ ):		18.12	244.283					
G323.74−00.26	1	2020 Aug 15	−187.1	−177.7	1.5	1.9	−0.268	0.239	1.232	2.139
	2	2020 Aug 21	−187.1	−177.7	1.5	1.9	−0.281	0.098	1.219	1.998
	3	2021 Feb 12	−188.3	−179.6	0.3	0.0	0.058	0.012	0.358	−0.012
	4	2021 Feb 18	−188.3	−179.6	0.3	0.0	−0.009	−0.143	0.291	−0.143
	5	2021 Feb 22	−188.3	−179.6	0.3	0.0	−0.020	−0.114	0.280	−0.114
	6	2021 Jul 28	−190.4	−181.4	−1.8	−1.8	−0.031	0.037	−1.831	−1.763
	7	2021 Aug 08	−190.4	−181.4	−1.8	−1.8	−0.089	−0.033	−1.889	−1.833
		Ref. pos. ( $\tilde{x}_T, \tilde{y}_T$ ):		−188.6	−179.6					

lead to a 20% increase in phase shifts (assuming the same value for the residual total electron content). This implies that there is likely to be an increased number of phase wraps in our 6.7 GHz data compared to those seen by Hyland et al. (2022).

In order to unwrap the phases, we took the minimum difference of phase between consecutive scans on the same calibrator when adding trial values of  $360^\circ$ ,  $0^\circ$ , and  $-360^\circ$ . Additionally, all phases were minimized relative to a common time at the center of the track, where the delay errors due to residual tropospheric and ionospheric errors are expected to be at a minimum.

Once unwrapped, the phase data on each scan were fit with the least-squares method to a model for a 2D plane (see Equation (5) from Hyland et al. 2022), and the interpolated phase at the origin was subtracted from the maser visibility data using the task CLCAL.

The maser reference channel was then imaged using the *AIPS* task IMAGR, and the brightness distribution was fitted with a Gaussian model using the task JMFIT in order to measure the astrometric offsets ( $x_m, y_m$ ) from the original phase center in Table 2.



**Figure 6.** Parallax and proper-motion modeling of the G323.74–00.26 velocity channel  $v = -50.52 \text{ km s}^{-1}$ . Left: total sky position change over the full observation period. Middle: decomposition of sky motion into east–west (green dotted–dashed line) and north–south (blue dashed line) motion over time. Right: parallax motion (i.e., proper-motion subtracted) over time. Error bars show independent  $1\sigma$  error floors for each direction as 25 and 39  $\mu\text{s}$  for the east–west and north–south directions, respectively.

**Table 3**  
Trigonometric Parallaxes and Proper Motions Determined from iPR from the Target Maser and iMV

Source		$\theta_{\text{sep}}$ (deg)	$\pi$ (mas)	$\mu_x$ (mas yr $^{-1}$ )	$\mu_y$ (mas yr $^{-1}$ )	Num. Epochs
Target	Background					
G232.62+00.99	J0735–1735	1.06	$0.523 \pm 0.055$	$-2.367 \pm 0.100$	$2.353 \pm 0.100$	6
	J0725–1904	2.58	$0.634 \pm 0.053$	$-2.221 \pm 0.098$	$2.155 \pm 0.204$	7
	J0729–1320	3.70	$0.636 \pm 0.048$	$-2.175 \pm 0.085$	$2.533 \pm 0.128$	6
	J0748–1639	3.81	$0.433 \pm 0.024$	$-2.252 \pm 0.043$	$2.958 \pm 0.142$	6
	J0730–1141 <sup>a</sup>	5.30	...	...	...	...
	iMV w/ all Inc. int. mot. <sup>b</sup>		$0.610 \pm 0.011$	$-2.266 \pm 0.021$ $-2.266 \pm 0.330$	$2.249 \pm 0.049$ $2.249 \pm 0.330$	7
G323.74–00.26	J1515–5559	2.36	$0.359 \pm 0.027$	$-3.25 \pm 0.08$	$-4.01 \pm 0.10$	7
	J1512–5640	2.60	$0.374 \pm 0.032$	$-3.23 \pm 0.09$	$-3.83 \pm 0.25$	7
	J1534–5351	2.68	$0.437 \pm 0.028$	$-3.20 \pm 0.08$	$-3.89 \pm 0.15$	7
	J1524–5903 <sup>c</sup>	2.71	...	...	...	3
	J1600–5811	4.18	$0.294 \pm 0.051$	$-3.06 \pm 0.14$	$-3.72 \pm 0.19$	7
	J1511–5203	5.37	$0.484 \pm 0.059$	$-3.57 \pm 0.18$	$-3.71 \pm 0.25$	6
	iMV w/ all Inc. int. mot.		$0.364 \pm 0.009$	$-3.239 \pm 0.025$ $-3.239 \pm 0.400$	$-3.976 \pm 0.039$ $-4.174 \pm 0.400$	7

**Notes.** The iMV results attained using data from all QSOs.

<sup>a</sup> The iPR from G232.62+00.99 to QSO J0730–1141 did not produce coherent synthesized images at any epoch.

<sup>b</sup> Including internal motions.

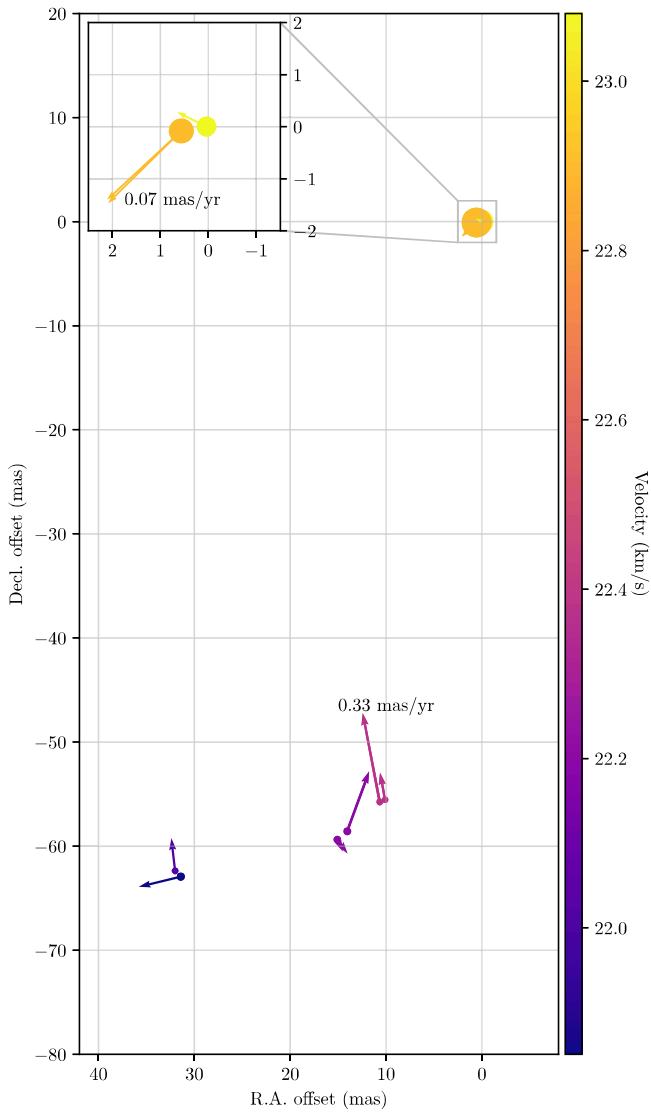
<sup>c</sup> The iPR from G323.74–00.26 to QSO J1524–5903 only produced coherent synthesized images at three out of seven epochs.

### 3.4. Position Shifting and Parallax Fitting

In order to minimize phase wraps (see the previous section), the (moving) maser position was updated at each observing season. In order to put the measured positions back into a stationary reference frame, one must undo these shifts before fitting the parallax and proper motion. To achieve this, we first chose a reference position shift from the correlated position:  $\tilde{x}_T, \tilde{y}_T$ . We then calculated the offset from this reference position at each epoch (i.e.,  $x_T - \tilde{x}_T$ ) and added it to the measured maser offset from the synthesized images ( $x_m, y_m$ ).

This gave the total offset from the reference position over time ( $x_{\text{tot}}, y_{\text{tot}}$ ). These values are given in Table 2.

We fit the ( $x_{\text{tot}}, y_{\text{tot}}$ ) data using the model of Equation (2) in the Appendix with variance-weighted least-squares to determine the parallax ( $\pi$ ) and proper motions ( $\mu_x, \mu_y$ ). Since astrometric uncertainty is usually dominated by systematic errors whose magnitude is not known a priori, we added “error floors” to the  $x$  and  $y$  data in quadrature. We independently varied these error floors to achieve a  $\chi^2$  per degree of freedom of unity for each coordinate. This approach is widely used in maser astrometry and is considered the most reliable method



**Figure 7.** Map of methanol maser spots in G232.62+00.99 and their proper motions relative to the reference spot at (0, 0). The features shown were detected in  $\geq 5$  epochs. In the top left corner, the zoomed-in section around (0, 0) shows the main emission region is a blended double. (The data used to create this figure are available.)

for estimating the uncertainties in  $\pi$ ,  $\mu_x$ , and  $\mu_y$  (Reid et al. 2009a). The models as fit to the astrometric data for each target are shown in Figures 5 and 6.

#### 4. Results

Using iMV, we measure the parallax and proper motion of the 6.7 GHz emission in G232.62+00.99 to be  $\pi = 0.610 \pm 0.011$  mas,  $\mu_x = -2.266 \pm 0.021$  mas yr $^{-1}$ , and  $\mu_y = 2.249 \pm 0.049$  mas yr $^{-1}$ . This yields a distance of  $d = 1.639 \pm 0.030$  kpc (i.e., parallax inversion  $d = 1/\pi$  with symmetric errors  $\sigma_d = \sigma_\pi/\pi^2$ ). For G323.74–00.26, we measure a parallax of  $\pi = 0.364 \pm 0.009$  mas and proper motion of  $\mu_x = -3.239 \pm 0.025$  and  $\mu_y = -3.976 \pm 0.039$  mas yr $^{-1}$ , yielding a distance of  $d = 2.747 \pm 0.068$  kpc.

In order to evaluate the astrometric improvement of iMV compared to standard (inverse) phase referencing using a single calibrator, we also estimated parallaxes relative to each quasar in each cluster. We find that the parallaxes based on individual

calibrators in the G232.62+00.99 cluster range from 0.433 to 0.636 mas, and those in the G323.74–00.26 cluster range from 0.294 to 0.484 mas. These results are consistent with systematic parallax shifts of magnitude  $\sim 0.05$  mas per degree of calibrator angular offset found by Reid et al. (2017). All of the parallax and proper-motion results are tabulated in Table 3.

## 5. Discussion

### 5.1. G232.62+00.99

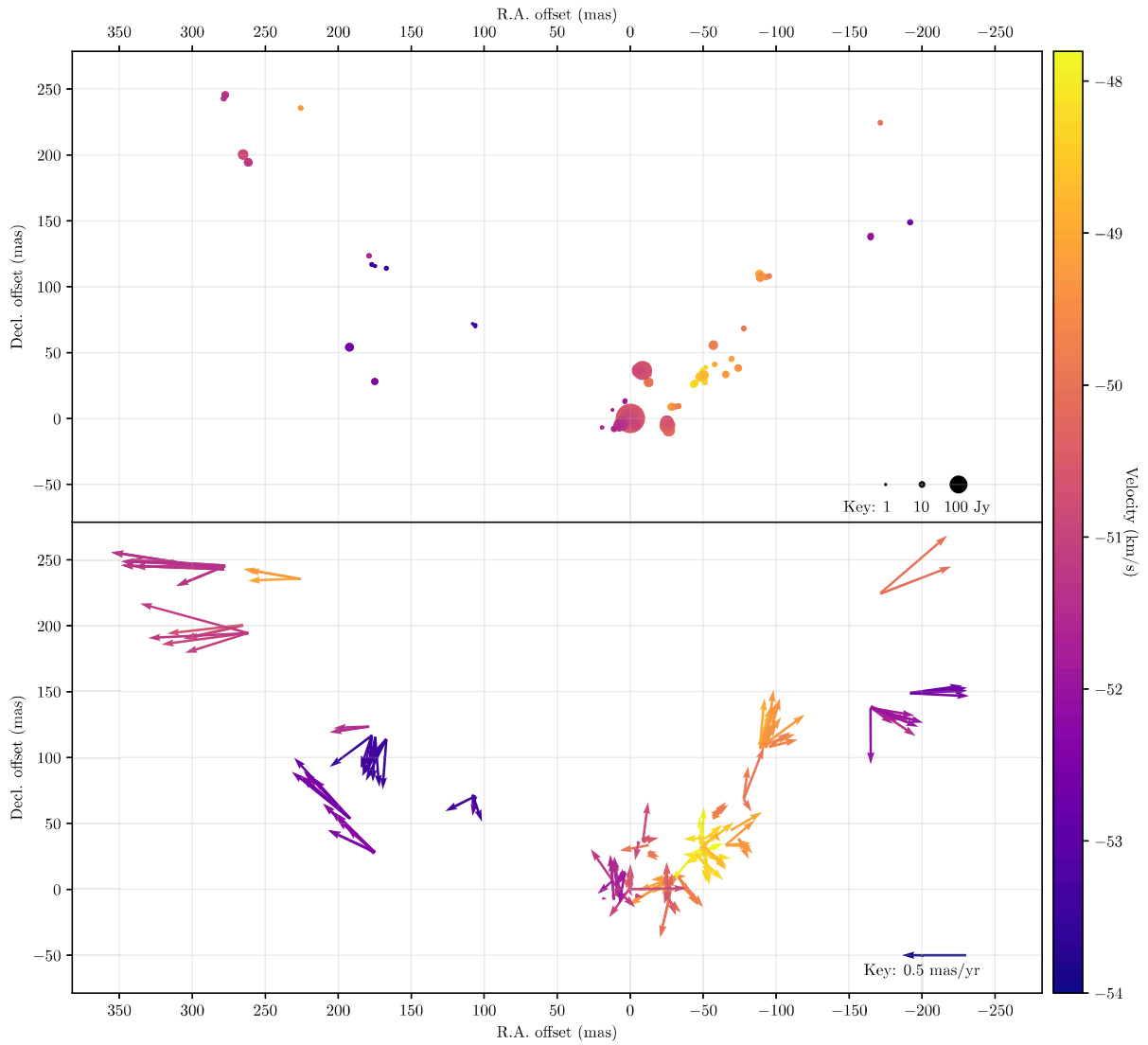
The parallax and proper motion of the 12 GHz methanol emission in G232.62+1.0 were measured with the VLBA between 2005 October and 2007 March to be  $\pi = 0.596 \pm 0.035$  mas,  $\mu_x = -2.17 \pm 0.06$  mas yr $^{-1}$ , and  $\mu_y = 2.09 \pm 0.46$  mas yr $^{-1}$  (Reid et al. 2009a). Compared to this previous measurement, the parallax and proper motions of the 6.7 and 12 GHz methanol masers agree within the quoted uncertainties, with the obvious difference being that the new estimate is three times more accurate for  $\pi$  and  $\mu_x$  and an order of magnitude more accurate for  $\mu_y$ .

It should be noted that the previous measurement was subject to issues that limited the performance of the VLBA; namely, the source was observed at very low elevations, the 12 GHz emission was resolved, and only the inner five VLBA antennas were used, limiting the maximum baseline length to 1500 km (compared to the maximum baseline we use of 4750 km). Accounting for the latter by simply dividing the previous parallax measurement uncertainty by  $\sim 3$  reduces it to  $\pm 12 \mu\text{as}$ . This indicates that we were able to successfully calibrate the delays (primarily the ionosphere) at 6.7 GHz to at least the same levels as could be achieved at 12 GHz, if not better.

The previous Southern Hemisphere 6.7 GHz methanol maser parallaxes were measured by Krishnan et al. (2015, 2017) on the Long Baseline Array, another Southern Hemisphere VLBI array that has common telescopes with the array that we used. These measurements were plagued by uncompensated dispersive delays, leading to parallaxes with accuracy between 50 and 110  $\mu\text{as}$ . Compared to the  $\sim 10 \mu\text{as}$  parallaxes we have measured, we can see that there has been a marked improvement owing to MV techniques.

The methanol maser emission toward G232.62+00.99 can be grouped into four regions, with the northernmost being the brightest. The regions are distributed in a slightly arched or linear arrangement and have a velocity gradient running southeast to northwest. The positions and internal motions relative to the reference feature are shown in Figure 7. The internal motions of the region relative to the reference maser feature are small, only  $\leq 0.33$  mas yr $^{-1}$  or  $2.6$  km s $^{-1}$  at the measured distance. This suggests that the internal motion of the reference feature is also small and that the measured proper motion of that feature is representative of the region as a whole. We have inflated the error in the region proper motion to  $0.33$  mas yr $^{-1}$  (Table 3) to account for this. The weakest consistently detected maser spot was 2 Jy, and the measured maser spot distribution is consistent with that reported by Fujisawa et al. (2014).

Object G232.62+00.99 well matches the ( $l$ ,  $b$ ) coordinates of the Local Arm as traced by Reid et al. (2019). The centroid velocity of the associated 6.7 GHz masers is near  $23$  km s $^{-1}$ , which compares reasonably with the  $17$  km s $^{-1}$  fitted to Local Arm sources nearby in angle.



**Figure 8.** Map and dynamics of maser spots in G323.74–00.26. Top: positions and flux densities of maser spots. Bottom: internal motions of maser spots. The features shown were detected in  $\geq 3$  epochs.

(The data used to create this figure are available.)

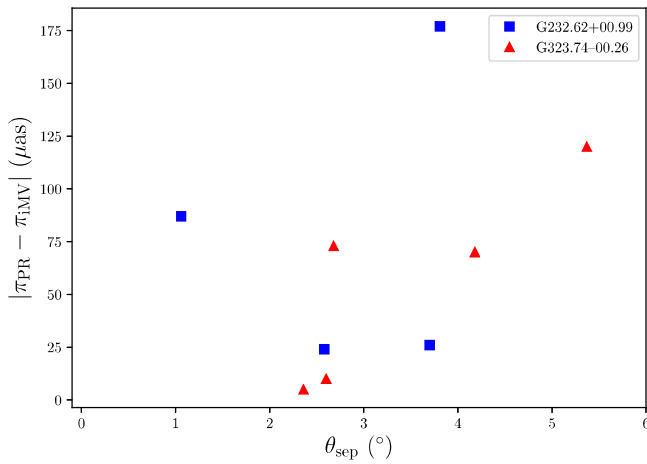
The center of the Local Arm at longitude  $232^\circ$  is at a distance of 0.83 kpc, and the estimated Gaussian  $1\sigma$  width of an arm at a galactocentric radius of 9 kpc is 0.4 kpc (Reid et al. 2019). At our measured distance of 1.64 kpc, this places G232.62+00.99 at 0.81 kpc (or about  $2\sigma$ ) from the arm center. Since this source is at one end (at Galactic azimuth  $-8^\circ$ ) of the sources with measured parallaxes used to trace the Local Arm, it could be that the pitch angle fitted over that azimuth range extending to the other end (azimuth  $+34^\circ$ ) should be increased slightly. Interestingly, however, there is a “bridge” of gas seen in H I starting at  $(l, V_{\text{lsr}}) = (232^\circ, 20^\circ \text{ km s}^{-1})$  and connecting to the Perseus arm at  $(242^\circ, 70^\circ \text{ km s}^{-1})$  (see Figure 12 of Reid et al. 2016). Possibly, G232.62+00.99 is associated with this bridge.

### 5.2. G323.74–00.26

Object G323.74–00.26 is clearly associated with the Scutum–Centaurus spiral arm, since its  $(l, b, V_{\text{lsr}})$  coordinates of  $(323.74^\circ, -0.26^\circ, -50 \text{ km s}^{-1})$  compare very well with the arm model of  $(323^\circ, -0.01^\circ, -53 \text{ km s}^{-1})$  of Reid et al. (2019).

That model places the center of the arm at this longitude at a distance of 3.2 kpc, which is about 0.45 kpc more distant than our parallax. At a galactocentric radius of 6.1 kpc, the arm width estimate of Reid et al. (2019) is 0.26 kpc, placing this source  $1.7\sigma$  from the center. However, given that at present, very few southern sources have accurate parallax measurements, this is not surprising, since the precise location of the Centaurus arm segment might be fairly uncertain at this time.

The G323.74–00.26 maser emissions arise from quite a large number of spots. Figure 8 shows the positions of bright spots and their apparent motions over time. We have subtracted the average apparent motion of  $\mu_{x_{\text{int}}} = 0.00 \pm 0.02$  and  $\mu_{y_{\text{int}}} = -0.198 \pm 0.012 \text{ mas yr}^{-1}$  in the R.A. and decl. directions, respectively. If the distribution of the measured spot motion is near-isotropic, this average will reflect the internal motion of the reference feature. Therefore, we also subtracted this motion from the measured proper motion of the reference feature measured with respect to the quasars (Table 3) to obtain an estimate of the absolute motion of the region, giving  $\mu_{x_{\text{tot}}} = -3.2 \pm 0.4$  and



**Figure 9.** Absolute difference between parallaxes determined with iMV and iPR for each maser.

$\mu_{\text{tot}} = -4.2 \pm 0.4 \text{ mas yr}^{-1}$ . Here we have added an additional uncertainty of  $0.4 \text{ mas yr}^{-1}$  in quadrature (equivalent to  $5 \text{ km s}^{-1}$  at the measured distance) to account for the likelihood that the spots do not have an isotropic velocity distribution. There does not seem to be significant evidence in favor of an edge-on disk structure, as has been suggested for this methanol maser (e.g., Phillips et al. 1998), and the structure and internal motions instead suggest that the maser spot distribution may be part of a bow shock.

The peculiar (noncircular) motion of G323.74–00.26 about the Galactic center of mass can be calculated from its measured 6D phase-space values. Adopting  $V_{\text{lsr}} = 50.5 \pm 5.0 \text{ km s}^{-1}$  and the rotation curve of Reid et al. (2019), we find  $(U_p, V_p, W_p) = (-5, -1, -8) \text{ km s}^{-1}$ , where  $U_p$  is toward the Galactic center at the position of the source,  $V_p$  is in the direction of Galactic rotation, and  $W_p$  is toward the north Galactic pole. Uncertainties from measurement error are  $\pm 5 \text{ km s}^{-1}$  in each coordinate, so G323.74–00.26 has a very small peculiar motion, as is typical for a young high-mass star.

### 5.3. Inverse MultiView

Comparing the parallax and proper-motion results from iMV with a group of calibrators to standard (inverse) phase referencing with a single calibrator (Table 3), we find that iMV is at least a factor of 2 better in accuracy. In Hyland et al. (2022), per-epoch positional uncertainties of  $\pm 20 \mu\text{as}$  were achieved at 8.3 GHz for calibrator separations of  $< 7^\circ$  in both the north–south and east–west directions. Here we report per-epoch positional uncertainties (determined from the error floor values) of  $\approx 26 \mu\text{as}$  in the east–west direction and  $\approx 50 \mu\text{as}$  in the north–south direction.

Figure 9 shows the difference between the iMV and inverse phase referencing (iPR) parallaxes as a function of total angular separation for both targets. Under the assumption that the iMV parallax is the true parallax, this plot shows the systematic error of iPR parallaxes versus target–calibrator separation. The behavior of the G323.74–00.26 iPR parallaxes is exactly as expected, where the error increases with target–calibrator separation. For G232.62+00.99, there is a larger spread and no clear trend. In both cases, all parallaxes based on different quasars have much more uncertain parallax fits.

Comparisons between the relative performance of iMV and iPR are inequitable because the experiments were specifically

tailored for iMV. However, in comparison with past 6.7 GHz parallax experiments (e.g., Krishnan et al. 2015, 2017; Reid et al. 2017), it is clear that our additional calibration steps have reduced the astrometric uncertainty and/or removed possible systematic errors that may have been introduced in the parallax fit.

It is important to note that for at least one quasar per maser, an iPR parallax was unable to be determined: once for the most distant calibrator (J1730–141), and the other for an intermediate distance calibrator (J1524–5903; Table 3). In both cases, the quasar in question was not visible in synthesized images at a number of epochs, presumably due to the uncalibrated delay slopes and perhaps additionally, in the case of J1524, low flux density.

For this reason, we stress the use of numerous compact and strong calibrators with good positions, which allow the original maser position to be updated despite the presence of uncalibrated delays (i.e., step 6 of preliminary reduction). It appears that five calibrators are the ideal number, allowing a balance between spatial and temporal sampling, while four calibrators should be considered the bare minimum. For specific linear arrangements of the target and calibrators, fewer may be acceptable.

## 6. Concluding Remarks

We have used the iMV calibration method to measure the parallax and proper motion of two 6.7 GHz class II methanol masers, with results approaching the highest accuracy ever achieved at this frequency.

As part of the S $\pi$ RALS project, we will continue to measure the parallaxes and proper motions for Southern Hemisphere 6.7 GHz class II methanol masers to fill in the fourth quadrant to better trace the spiral arms of the Milky Way. Based on the current array capabilities and preliminary surveys of compact maser emission on VLBI baselines (Hyland 2021), we estimate that there are at least 20 masers that are bright and compact enough to measure parallax with iMV in the current iteration of S $\pi$ RALS. We also aim to explore the application of direct MV (Rioja et al. 2017) to measure the parallaxes and proper motions of the weaker methanol masers inappropriate for iMV, which may double the number of possible targets.

## 7. Data and Code Availability

The data underlying this article will be shared on reasonable request to the corresponding author. The scripts and programs used for data reduction and calibration are available at <https://github.com/lucasjord/spirals/script>. The data behind Figures 1, 2, 7, and 8 are available at [https://github.com/lucasjord/spirals/imultiview\\_p2](https://github.com/lucasjord/spirals/imultiview_p2).

## Acknowledgments

This research was supported by the Australian Research Council (ARC) Discovery grant No. DP180101061. We want to thank Mr. Brett Reid and Mrs. Bev Benson for maintaining and organizing the University of Tasmania radio telescopes. We acknowledge the Jawoyn, Paredarerme, and Wiriangu peoples as the traditional owners of the land situating the Katherine, Hobart, and Ceduna telescopes, respectively. The Warkworth 30 m radio telescope is funded and operated by the Auckland University of Technology; we would like to thank Mr. Lewis Woodburn for the maintenance and management of this facility to enable its involvement in this project. This

research has made use of NASA's Astrophysics Data System Abstract Service. This research made use of MaserDB.net, an online database of astrophysical masers (Ladeyschikov et al. 2019). This research made use of Astropy, a community-developed core Python package for astronomy (Astropy Collaboration et al. 2013, 2018).














## Appendix

The model used to predict the position of the target ( $x, y$ ) at any given time ( $t$ ) relative to some reference time ( $t_0$ ) due to parallax ( $\pi$ ) and proper motion ( $\mu_x, \mu_y$ ) is as follows:

$$\begin{aligned} x &= \pi(Y \cos \alpha - X \sin \alpha) + \mu_x(t - t_0) \\ y &= \pi(Z \cos \delta - X \cos \alpha \sin \delta \\ &\quad - Y \sin \alpha \sin \delta) + \mu_y(t - t_0), \end{aligned} \quad (2)$$

where  $\alpha$  and  $\delta$  are the R.A. and decl. of the target, and  $X, Y, Z$  is the Earth's position relative to the Sun at epoch  $t$  (as determined by the NOVAS subroutines; Kaplan et al. 1989). Since the NOVAS routines request  $t$  in MJD, the  $\mu$  values are returned in milliarcsecond per day.

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